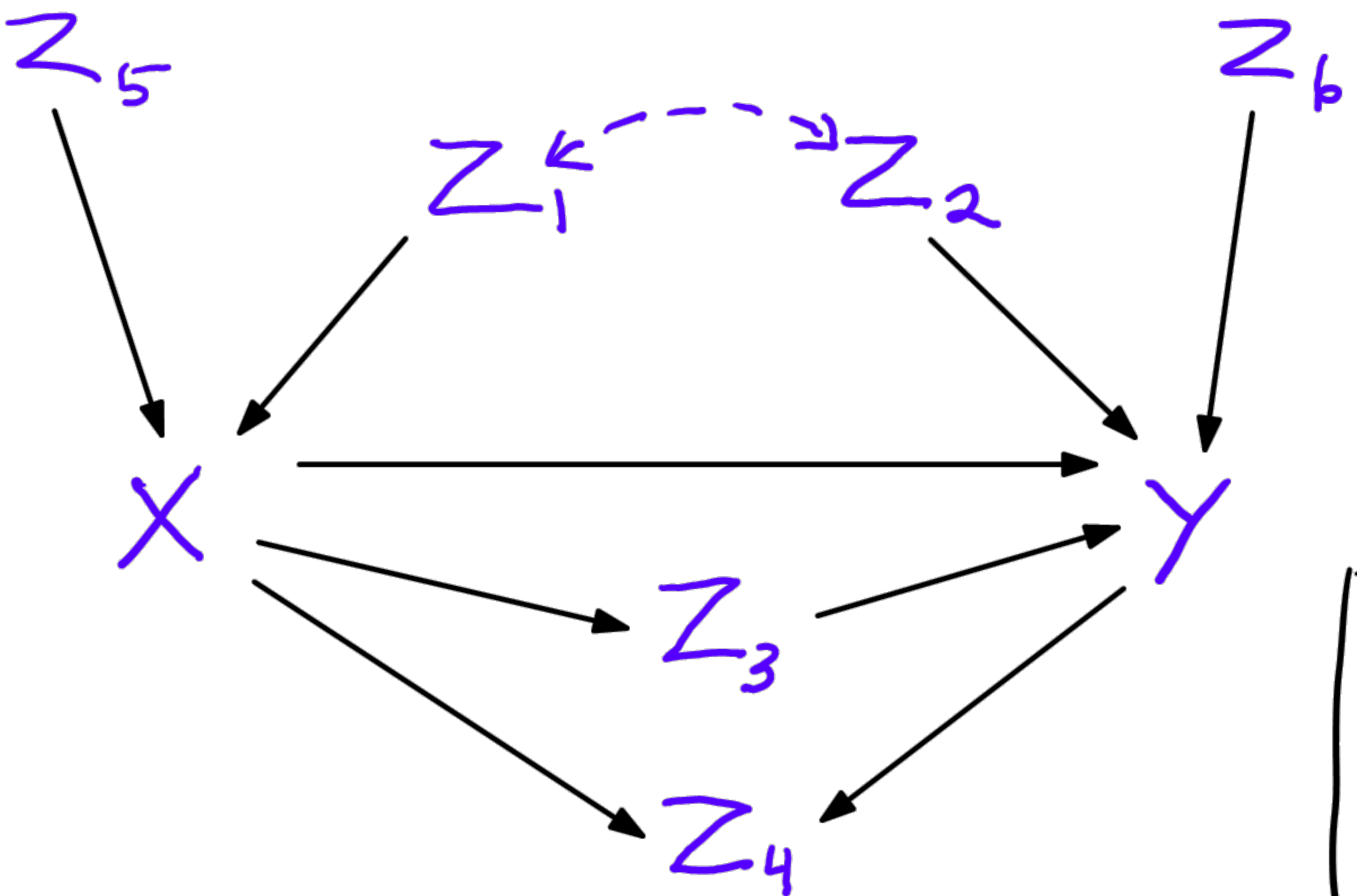
Does X cause Y?

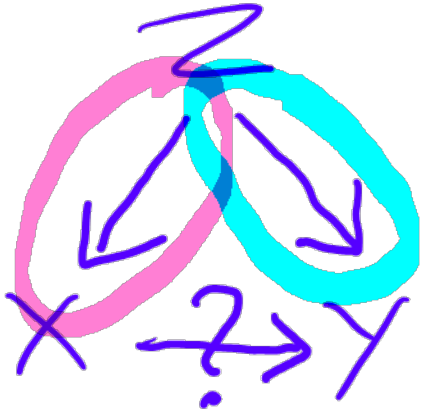
- A bird's eye view of methods with observational data
- Lord's Paradox and the role of longitudinal data

Causal Graph

Pearl & Mackenzie (2019)

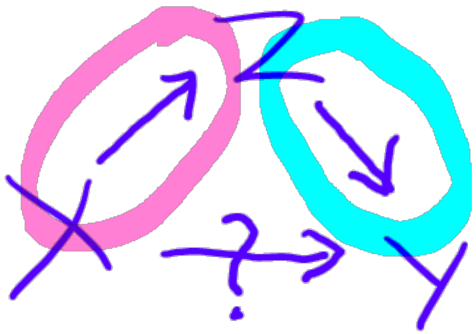


DAG = Directed acyclic graph



confounder

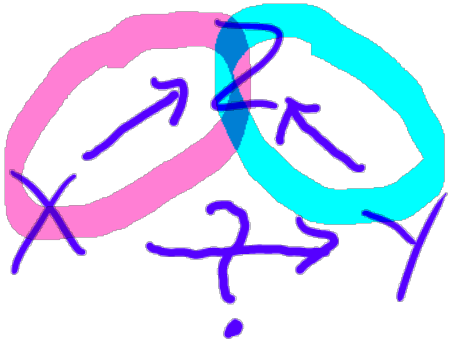
must include to see
see causal effect
of X on Y



mediator

must exclude

including may
wipe out a true effect



collider

e.g.
selection

must exclude

including may
create the impression
of an effect although there is
none

Moderators?

Can have - confounder-moderators
- mediator-moderators
- collider-moderators

Also mediator-colliders, etc
BUT not represented by DAGs

- So convenient visualizations of DAG are useful abstraction but limited in practice

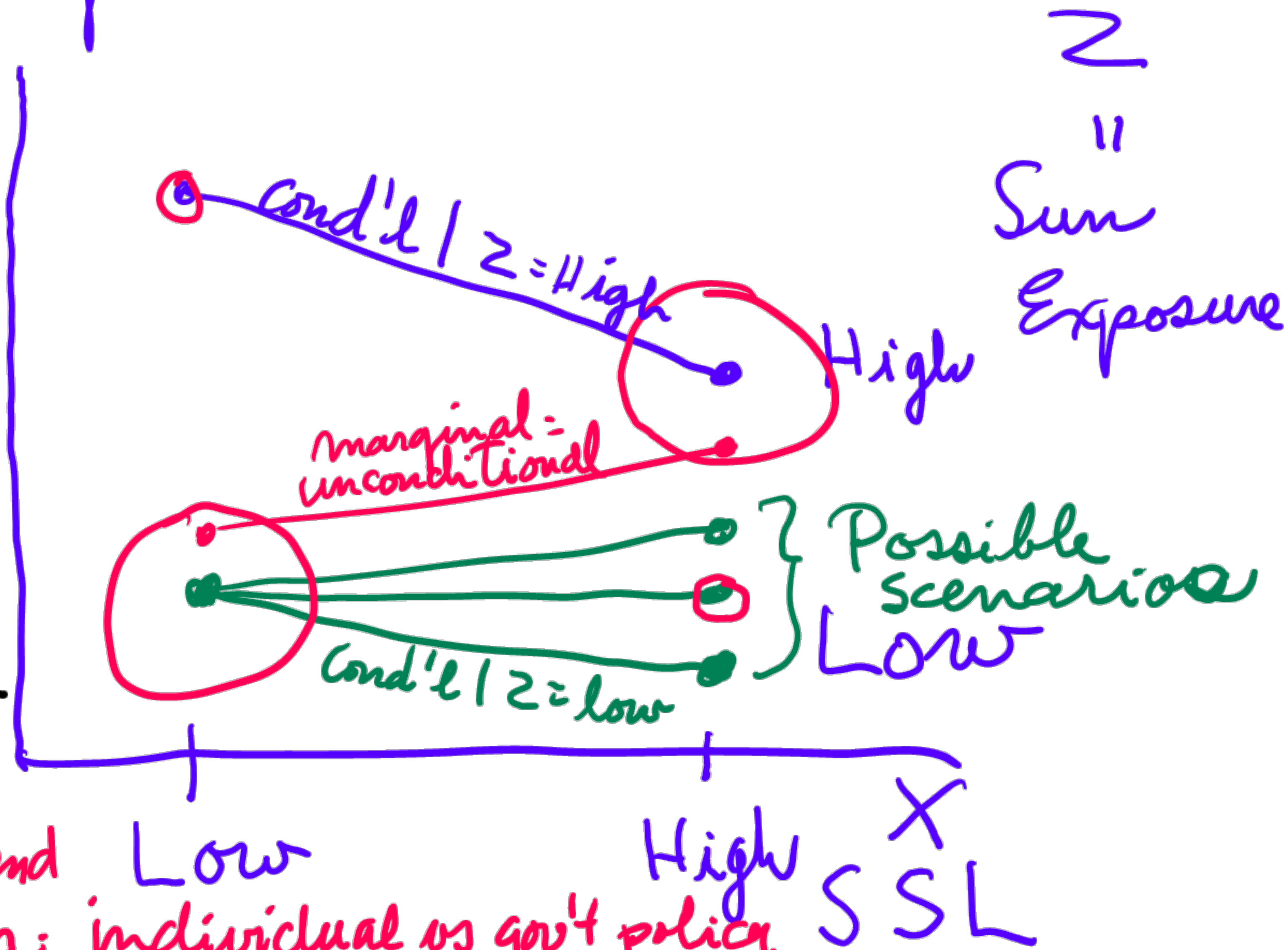
- avoiding inclusion of mediators more critical than avoiding colliders since inclusion of other confounders can correct for inclusion of a collider.

Moderator (= interaction) in data space

SSL example

Y

P(Skin Cancer)



"Moderator"

Cond'l lines not parallel

Role {Mediator / Confounder} of variable can depend on level of analysis: individual vs gov't policy

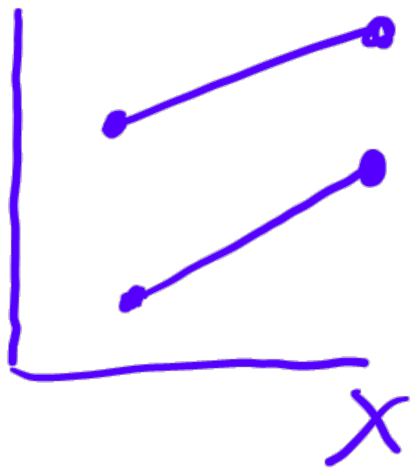
Moderation may be removable by monotonically transforming Y

if 1) Cond'l effects in same direction

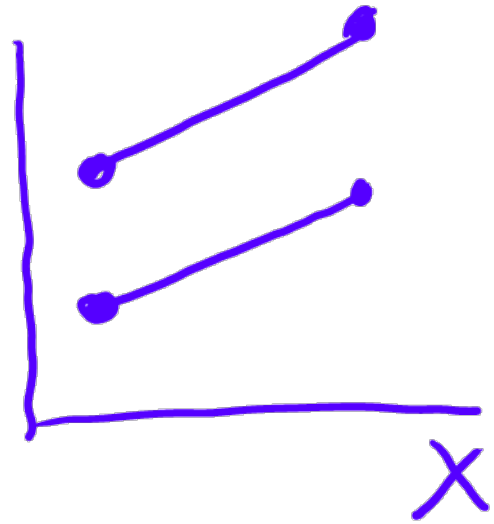
2) No crossings of lines

Removable

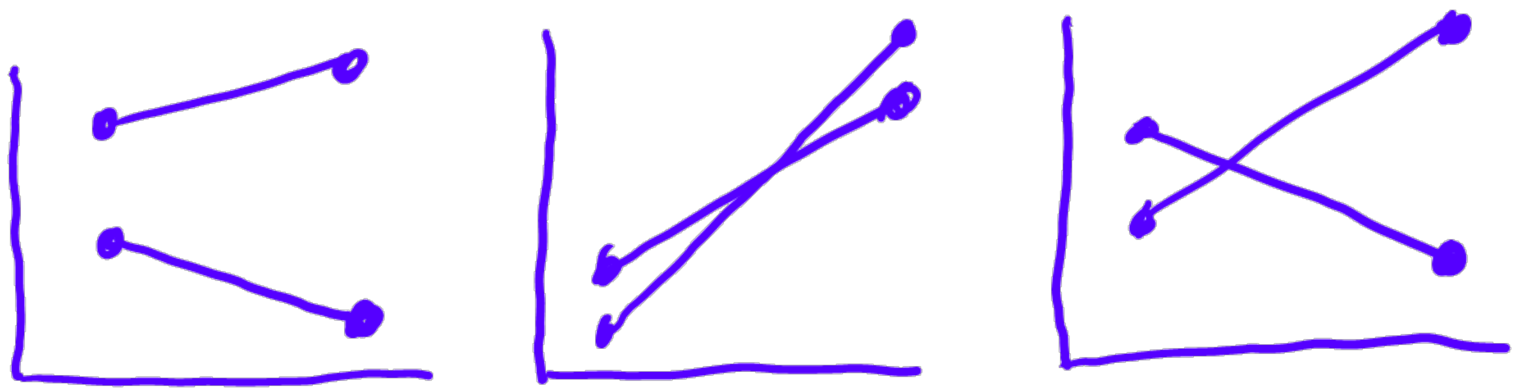
P(Y)



log odds $= \log\left(\frac{P(Y)}{1-P(Y)}\right)$



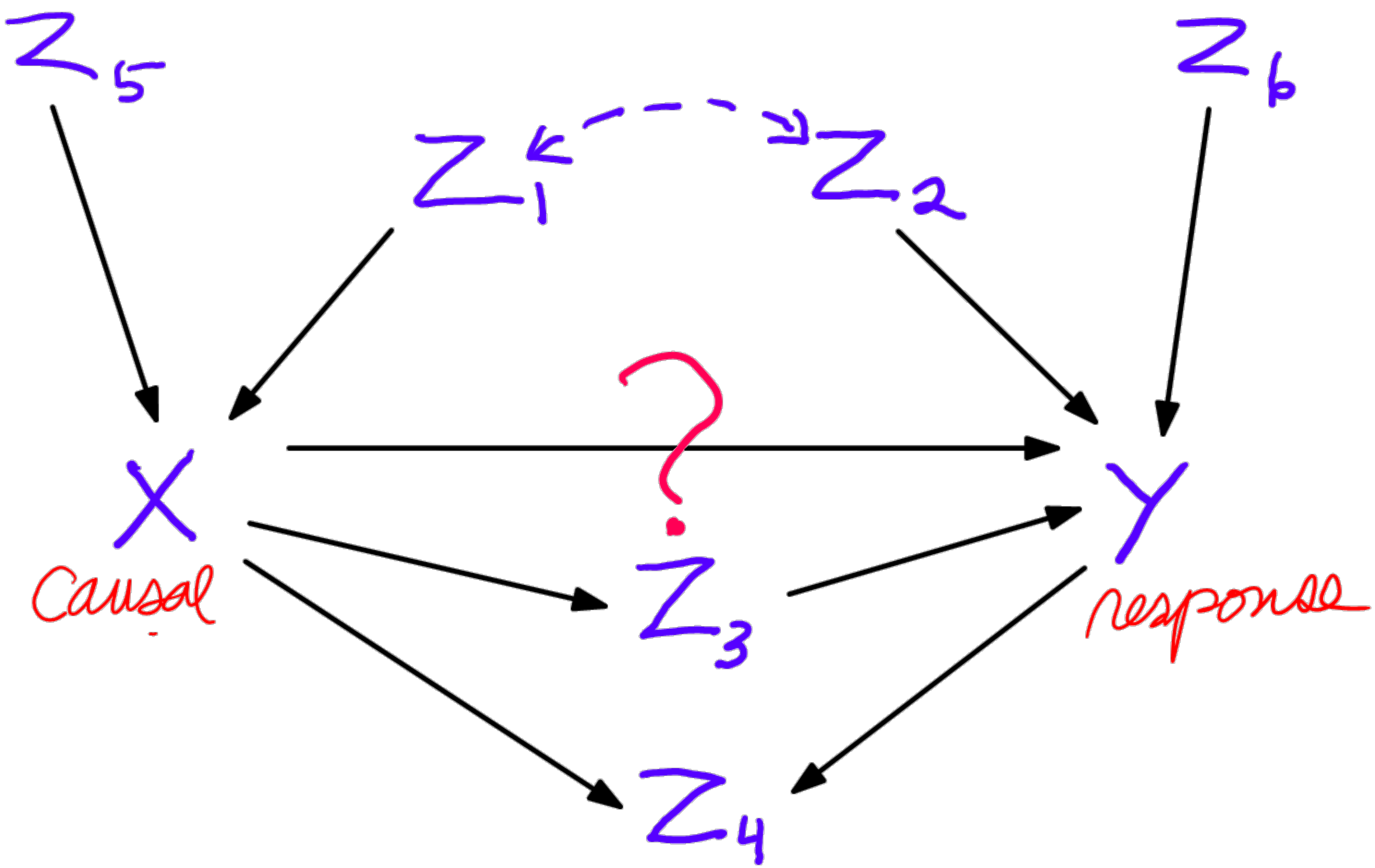
Nonremovable



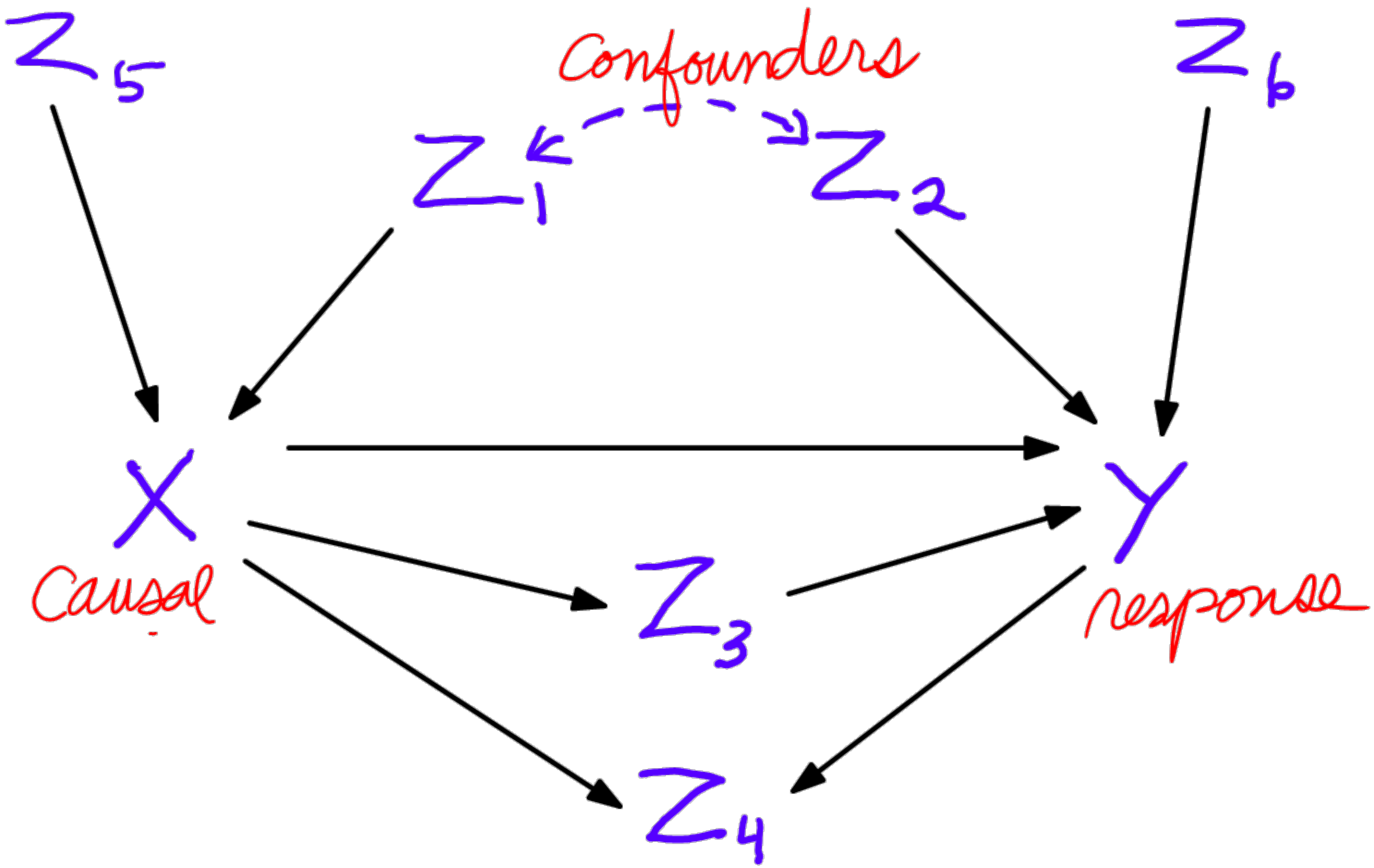
Note:

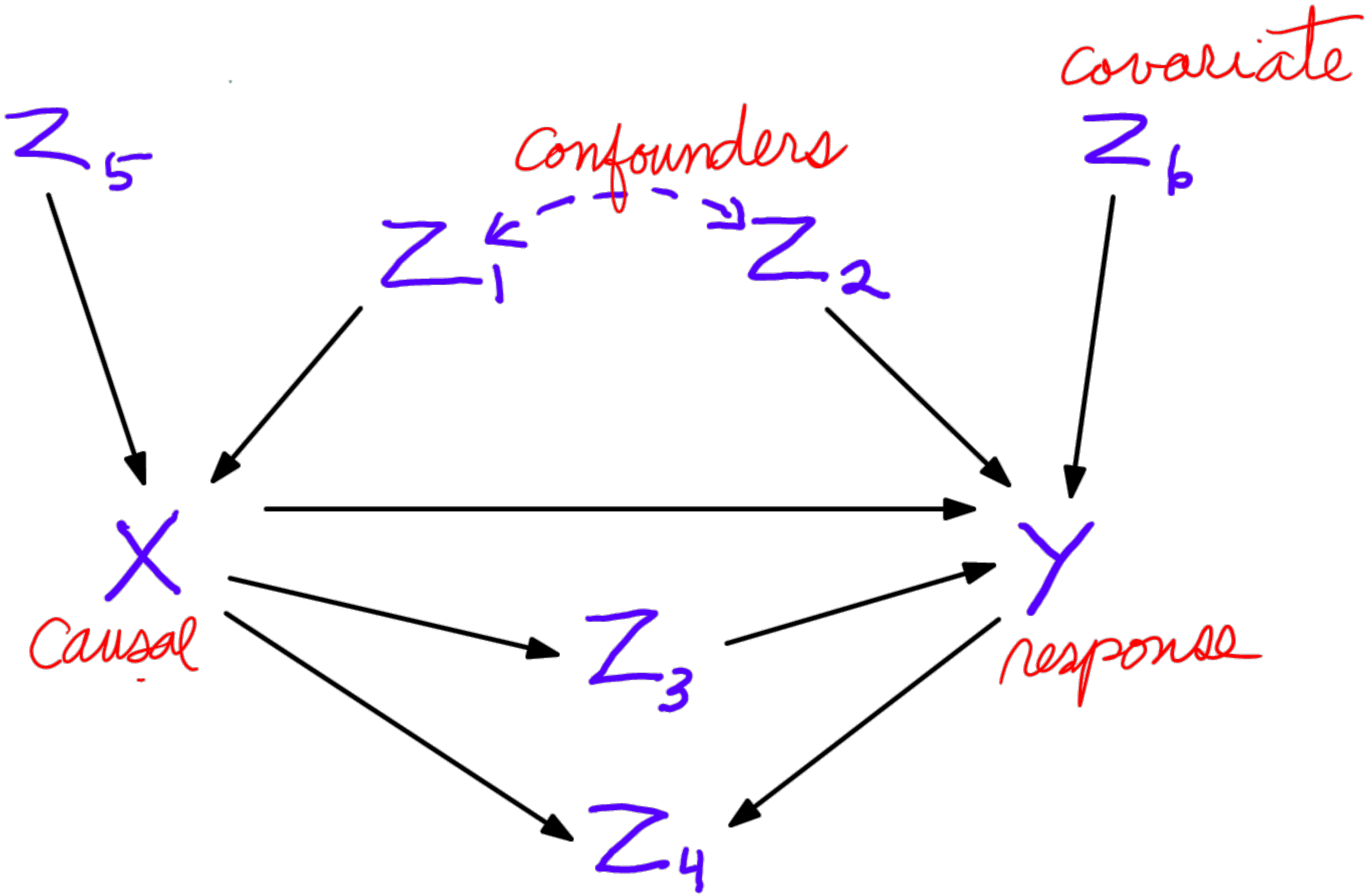
- Simpson effect: reversal of cond'l vs. marginal effects
- Moderation (= interaction in relation of X and Z with Y)
- Association (predictive)
- Causality

are distinct but not unrelated concepts



Z5
Z6
Z1
Z2
?
X
Y
Causal
response
Z3
Z4


Z_5
Confounders
Z_6
Z_1
Z_2
X
Y
Causal
response
Z_3
Z_4


covariate
Z_5
Confounders
Z_1
Z_2
Z_6
X
Y
Causal
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response
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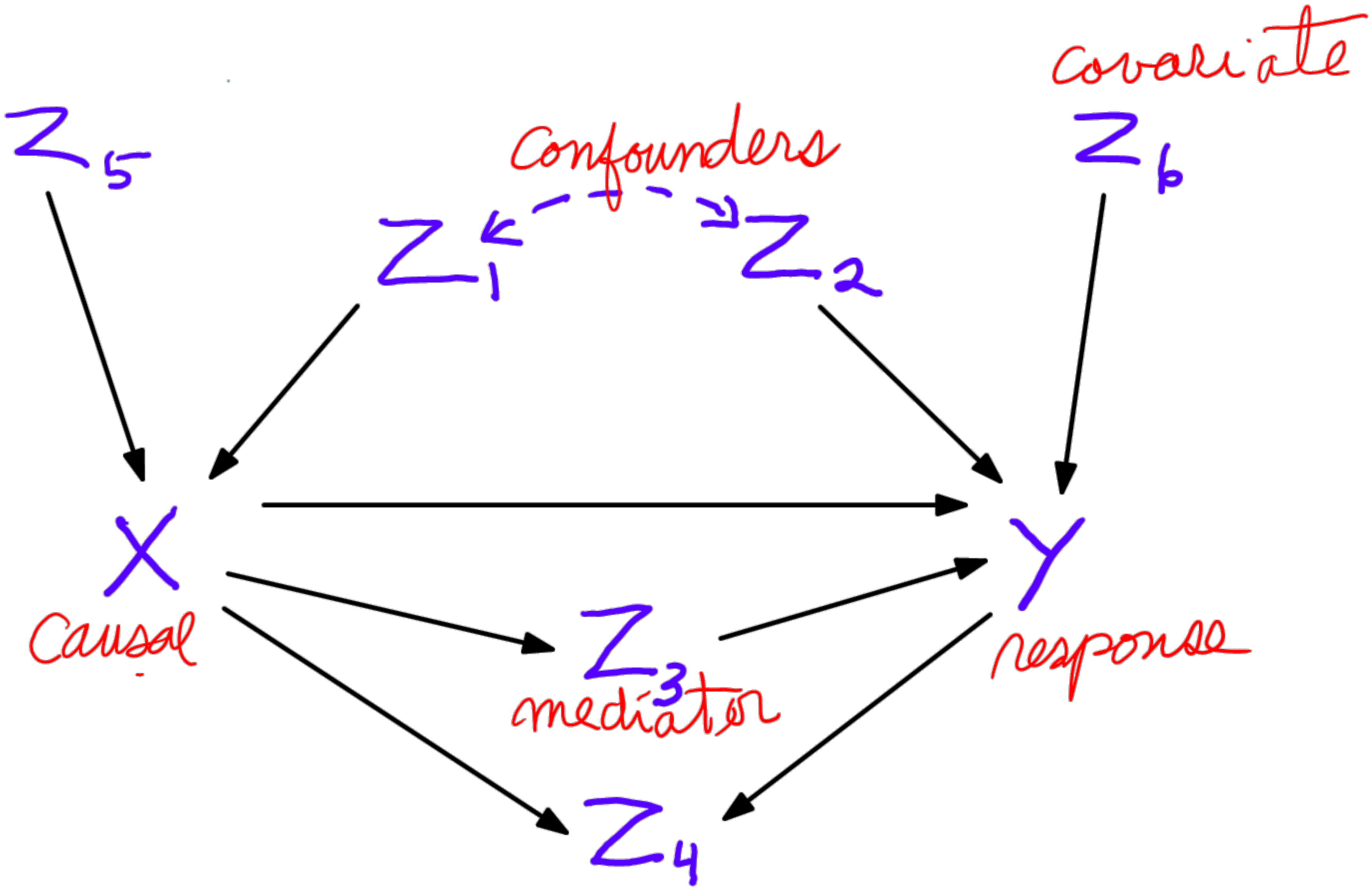
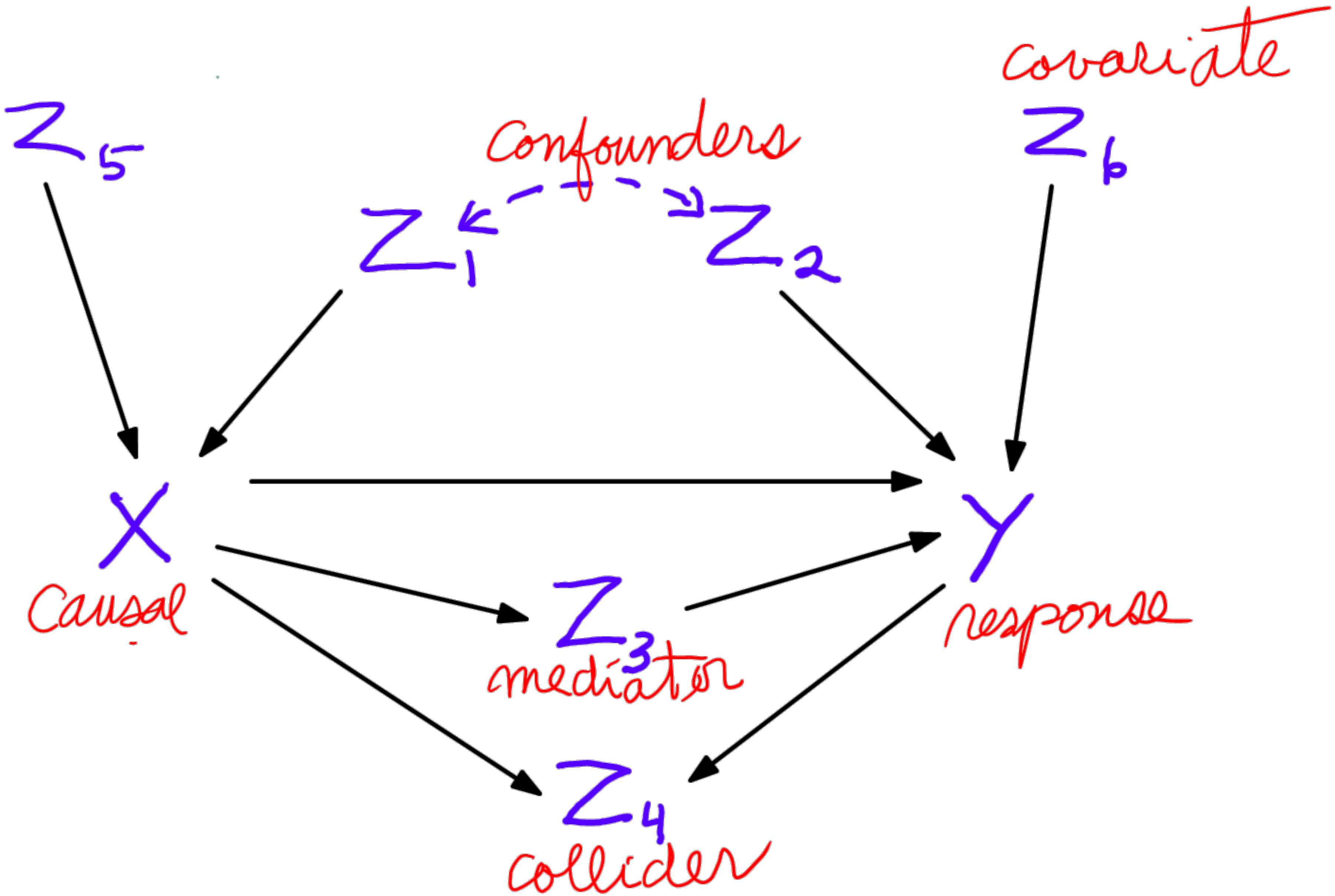
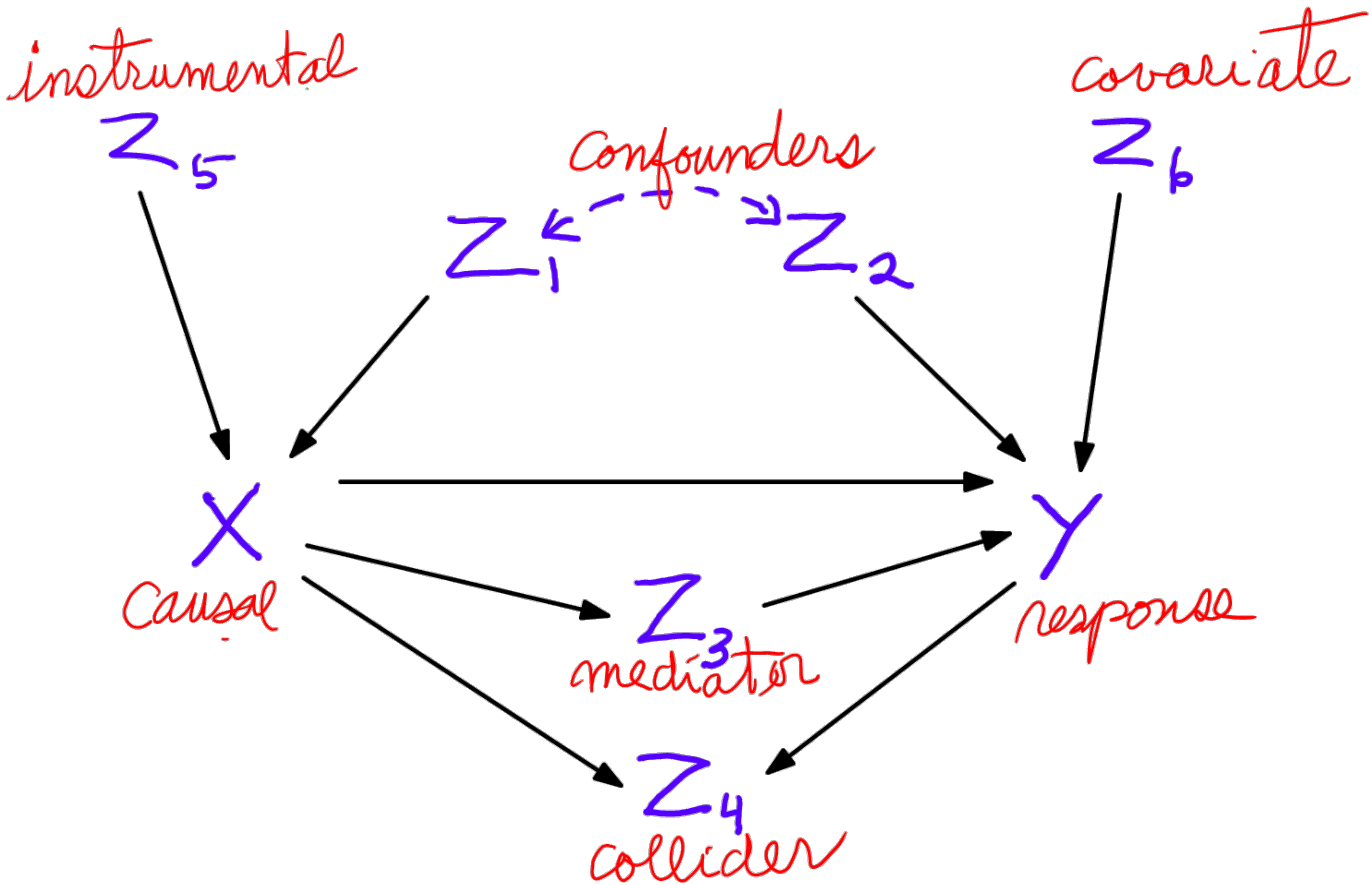
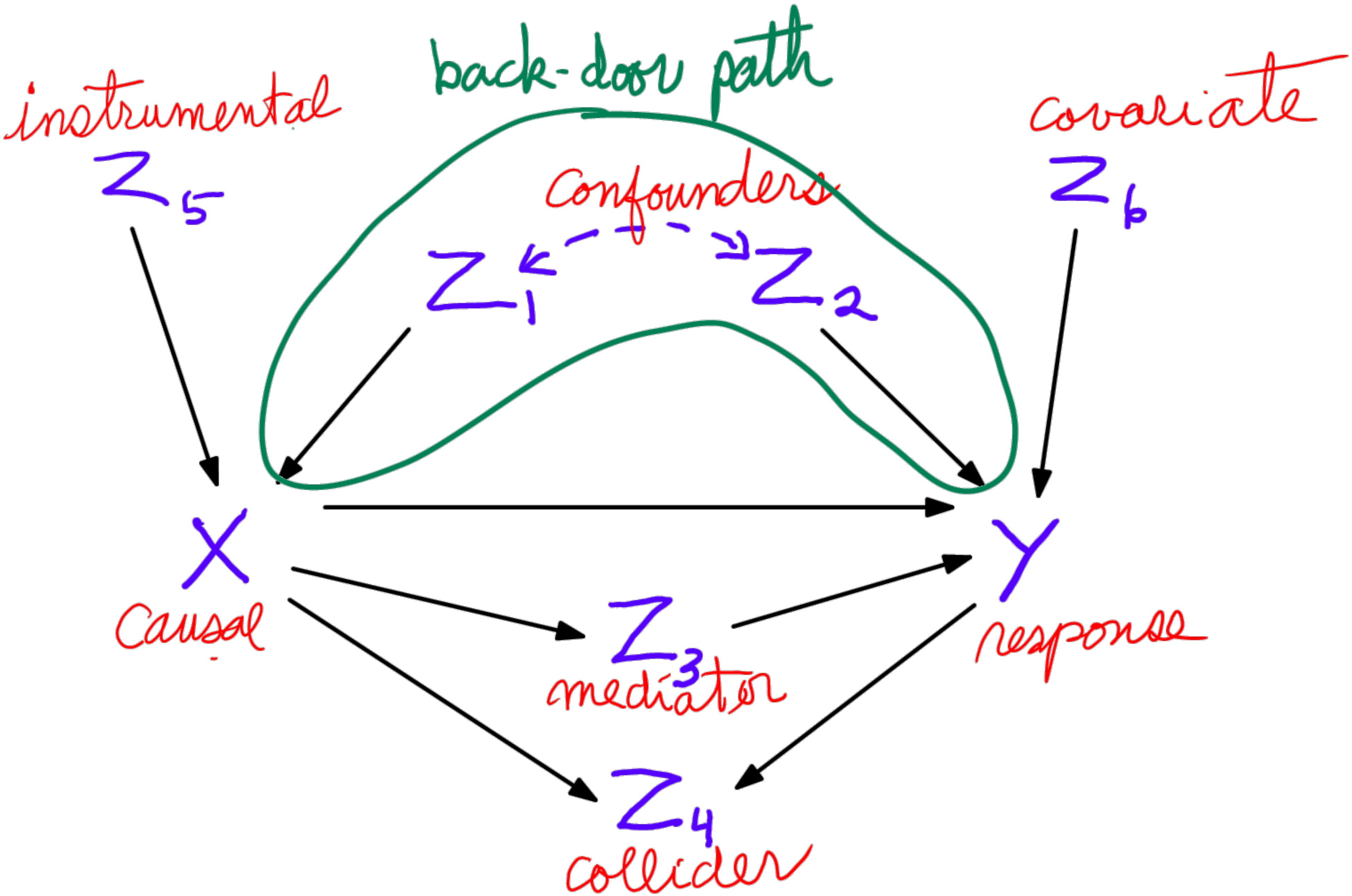


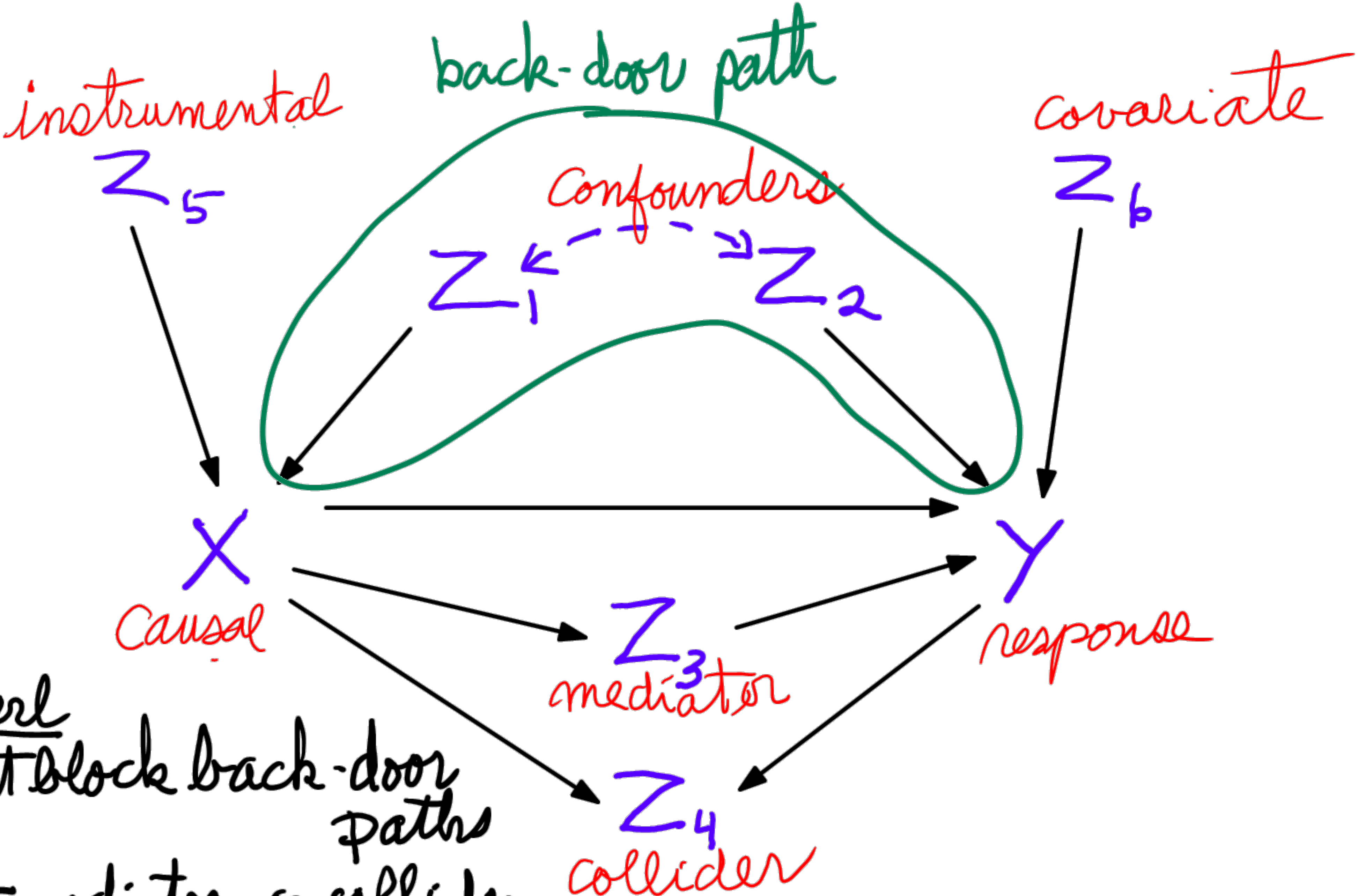
covariate
Confounders
Z_5
Z_1
Z_2
Z_6
X
Y
Causal
response
Z_3
mediator
Z_4



covariate
Z_5
Confounders
Z_1
Z_2
Z_6
X
Causal
Y
response
Z_3
mediator
Z_4
collider

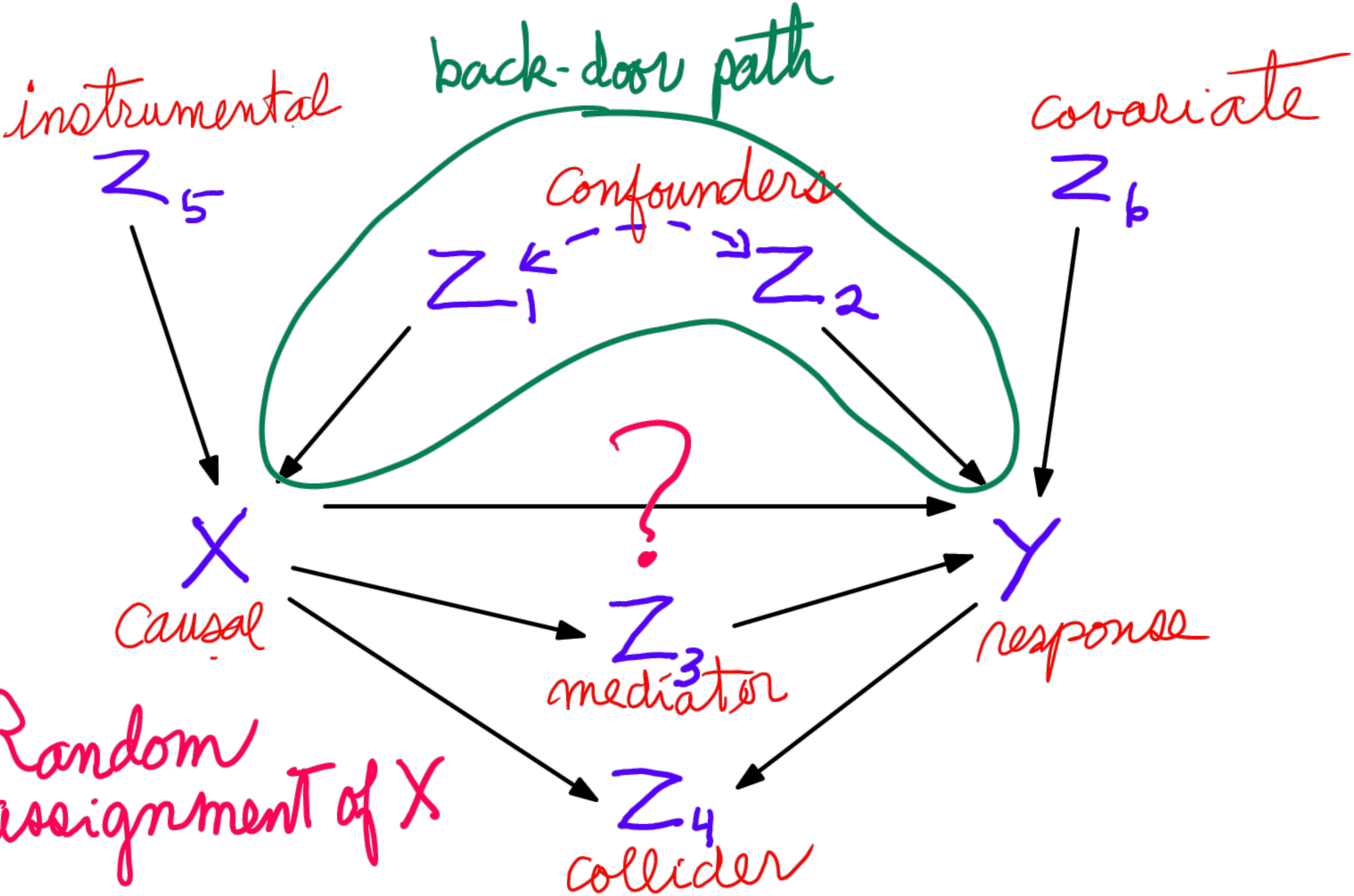

instrumental
Z_5
confounders
Z_1
Z_2
covariate
Z_6
X
causal
Y
response
Z_3
mediator
Z_4
collider


back-door path
instrumental
Z_5
confounders
Z_1
Z_2
covariate
Z_6
X
causal
Y
response
Z_3
mediator
Z_4
collider

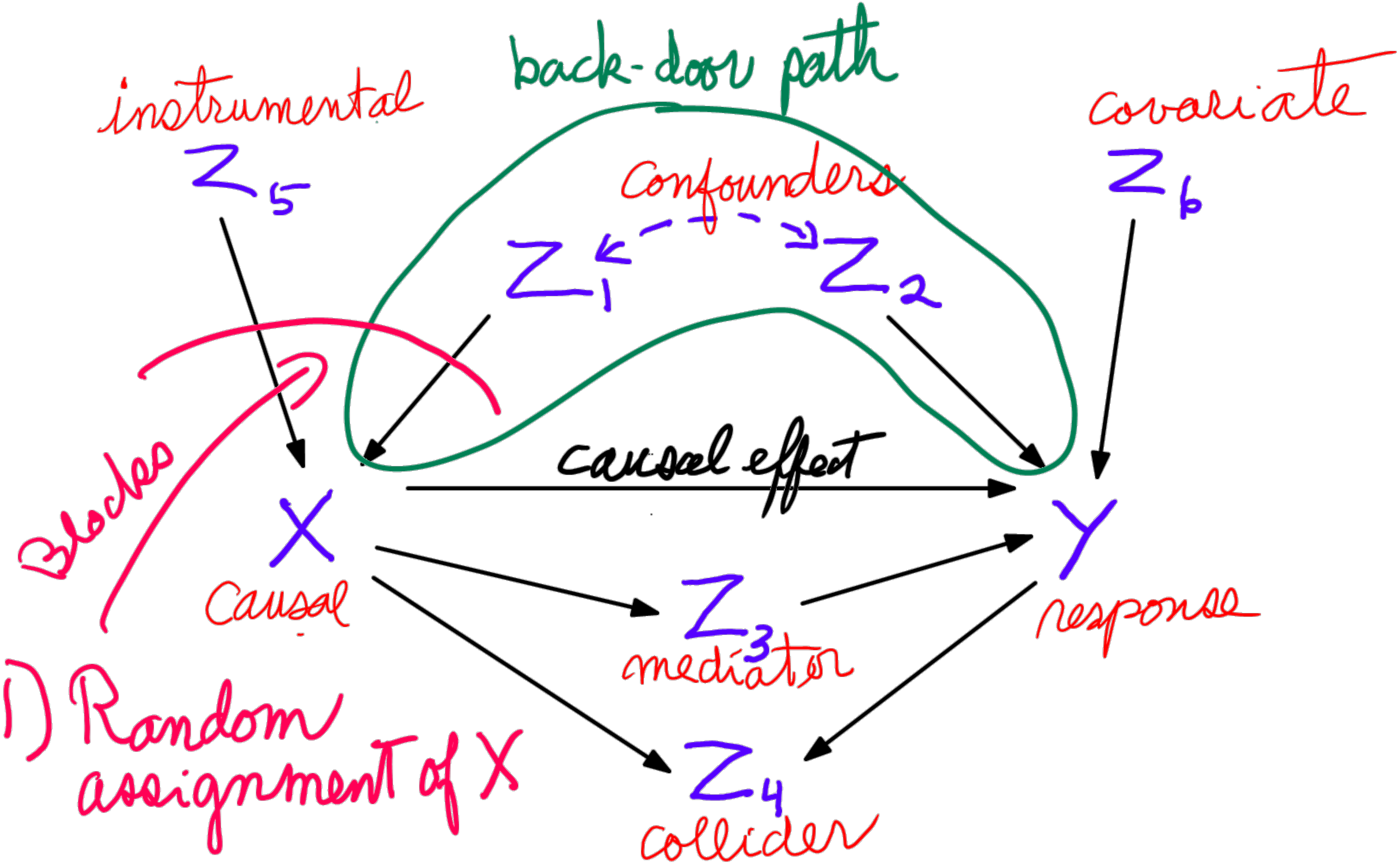


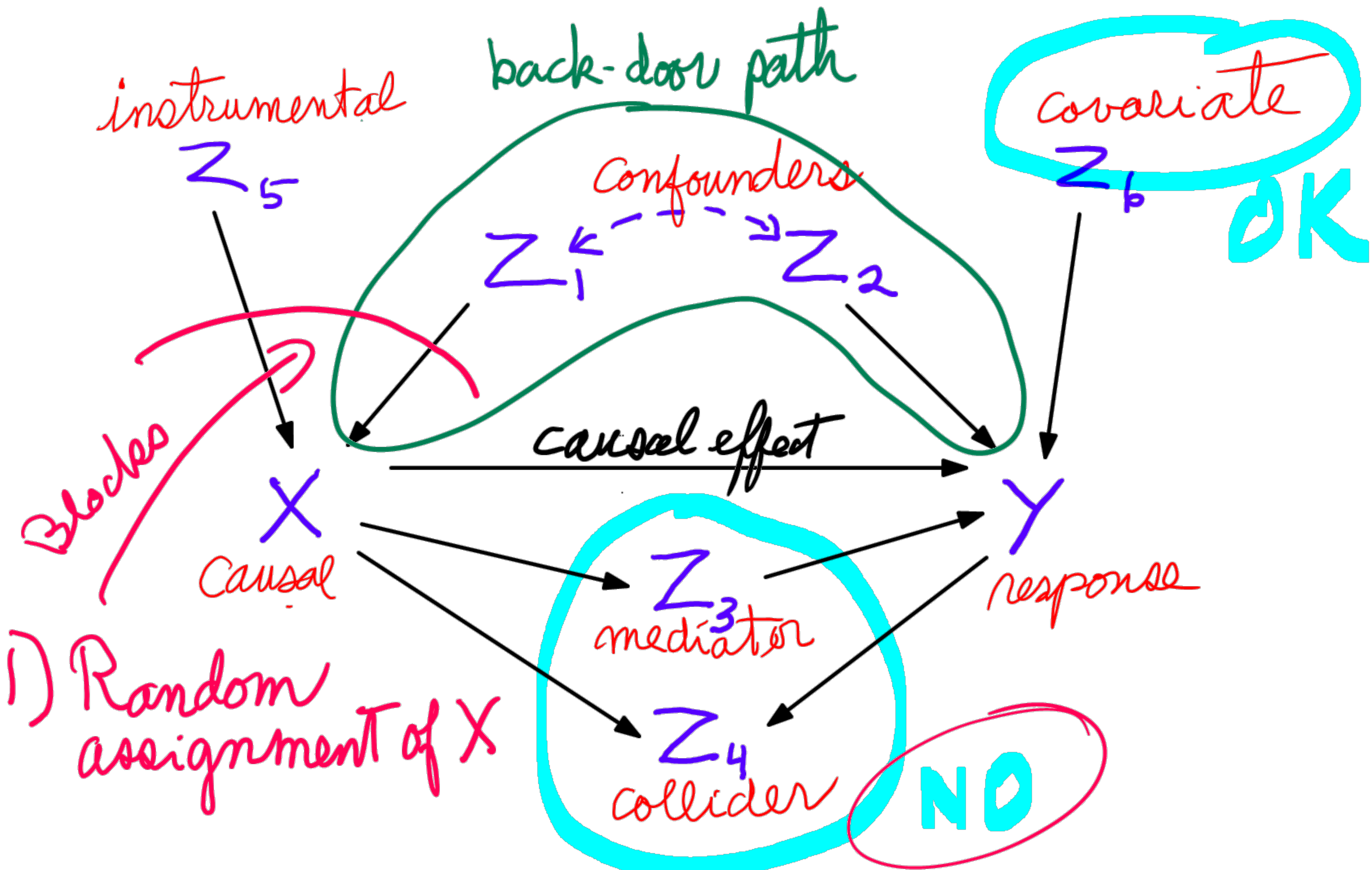
Pearl

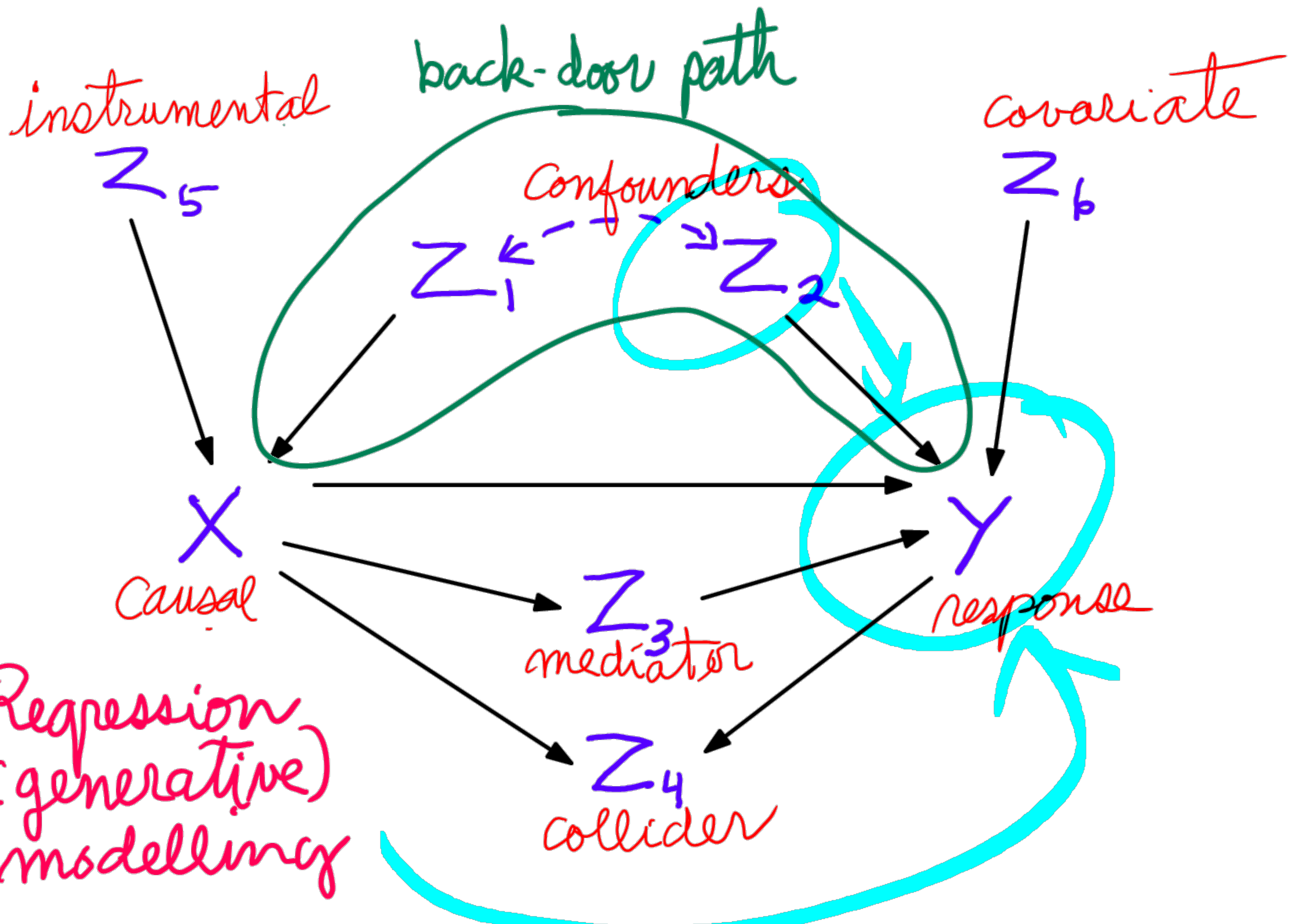
- Must block back-door paths
- NOT mediator or collider



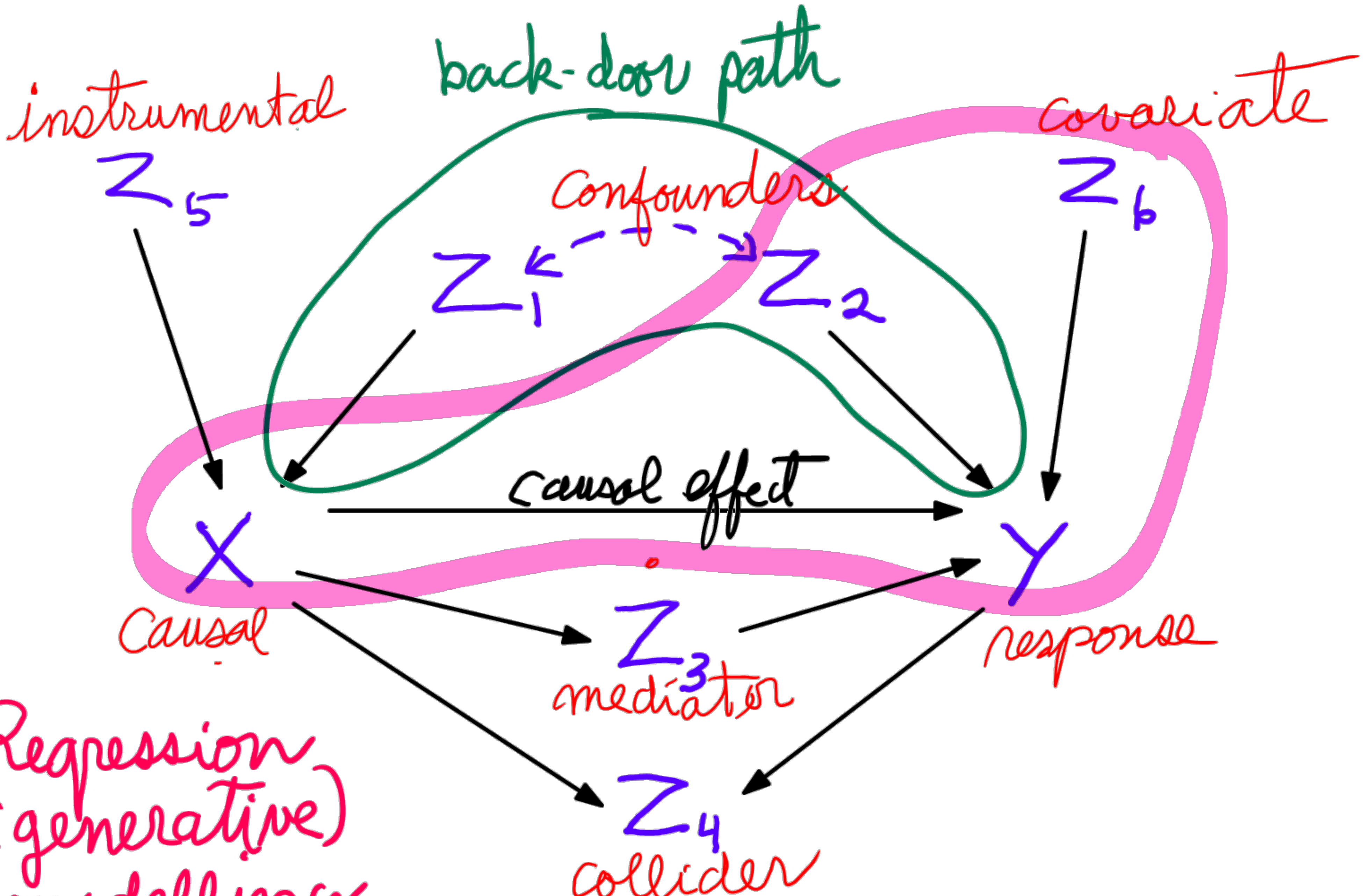
1) Random assignment of X


back-door path
instrumental
Z_5
Confounders
Z_1
Z_2
covariate
Z_6
Blocks
causal effect
X
causal
Y
response
Z_3
mediator
Z_4
collider
1) Random assignment of X

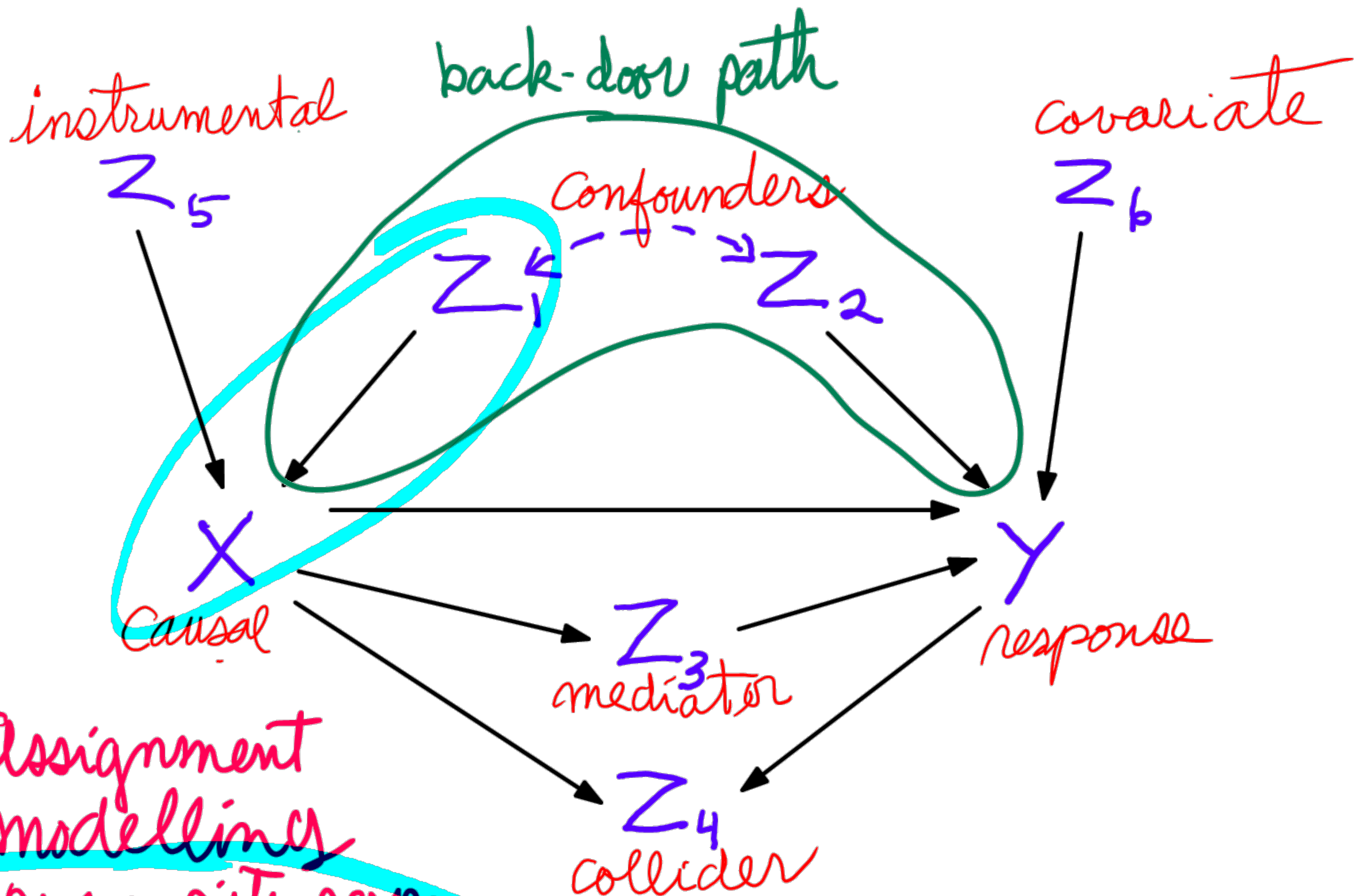

back-door path
instrumental
Z_5
confounders
Z_1
Z_2
covariate
Z_6
OK
Blocks
causal effect
X
causal
Y
response
Z_3
mediator
Z_4
collider
NO
1) Random assignment of X



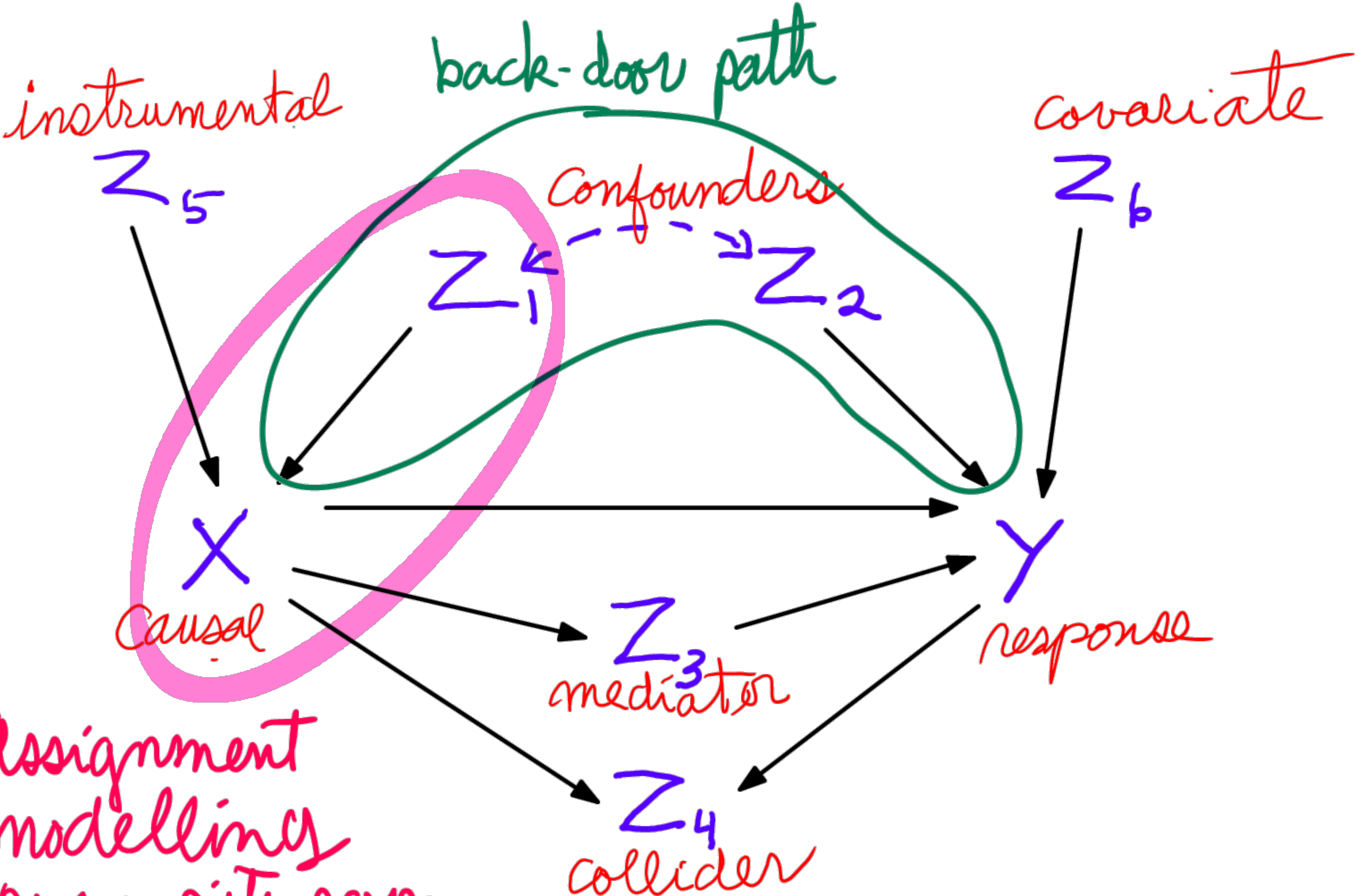
2) Regression (generative) modelling



2) Regression (generative modelling)



3) Assignment modelling
– propensity scores



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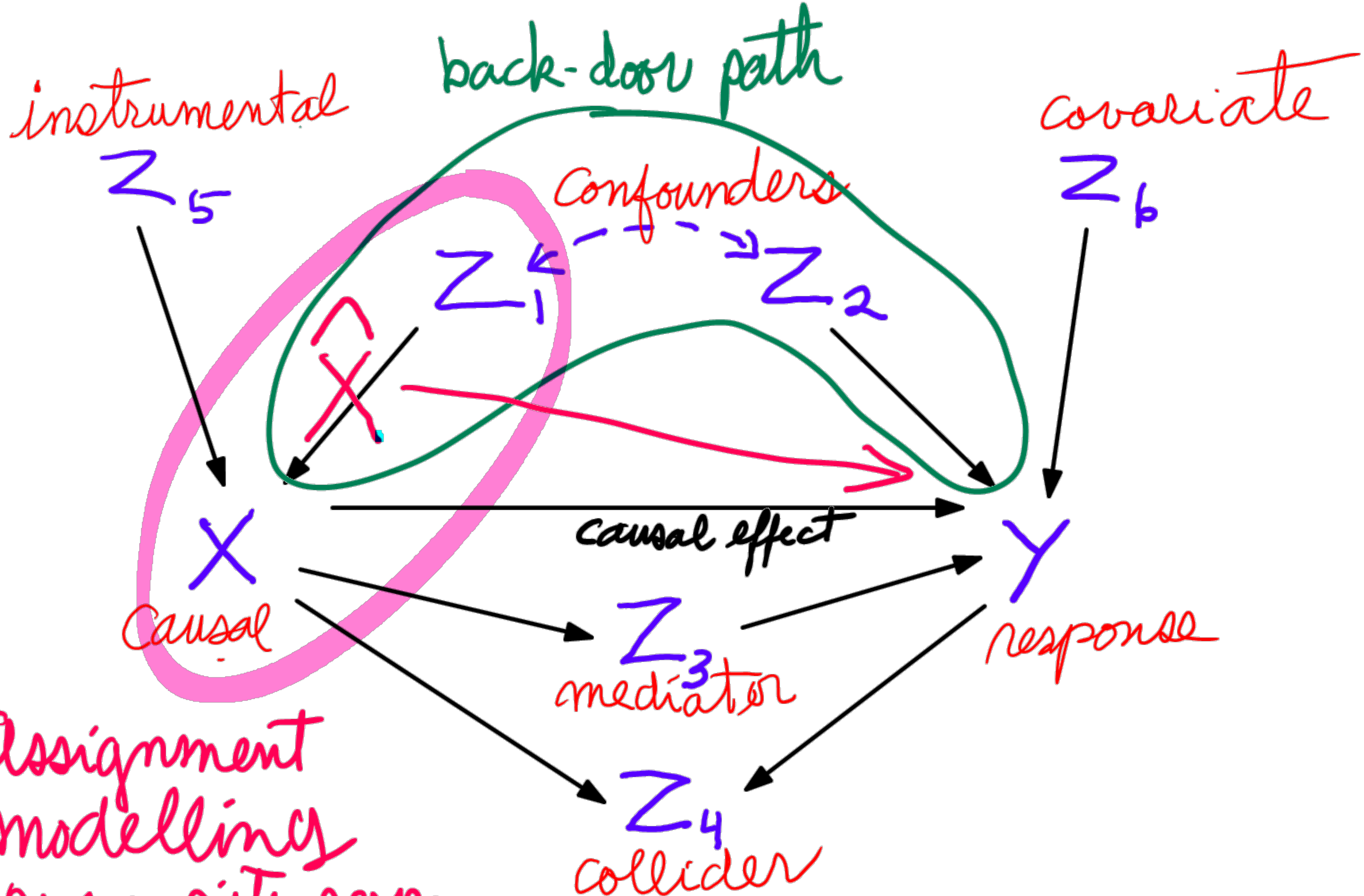

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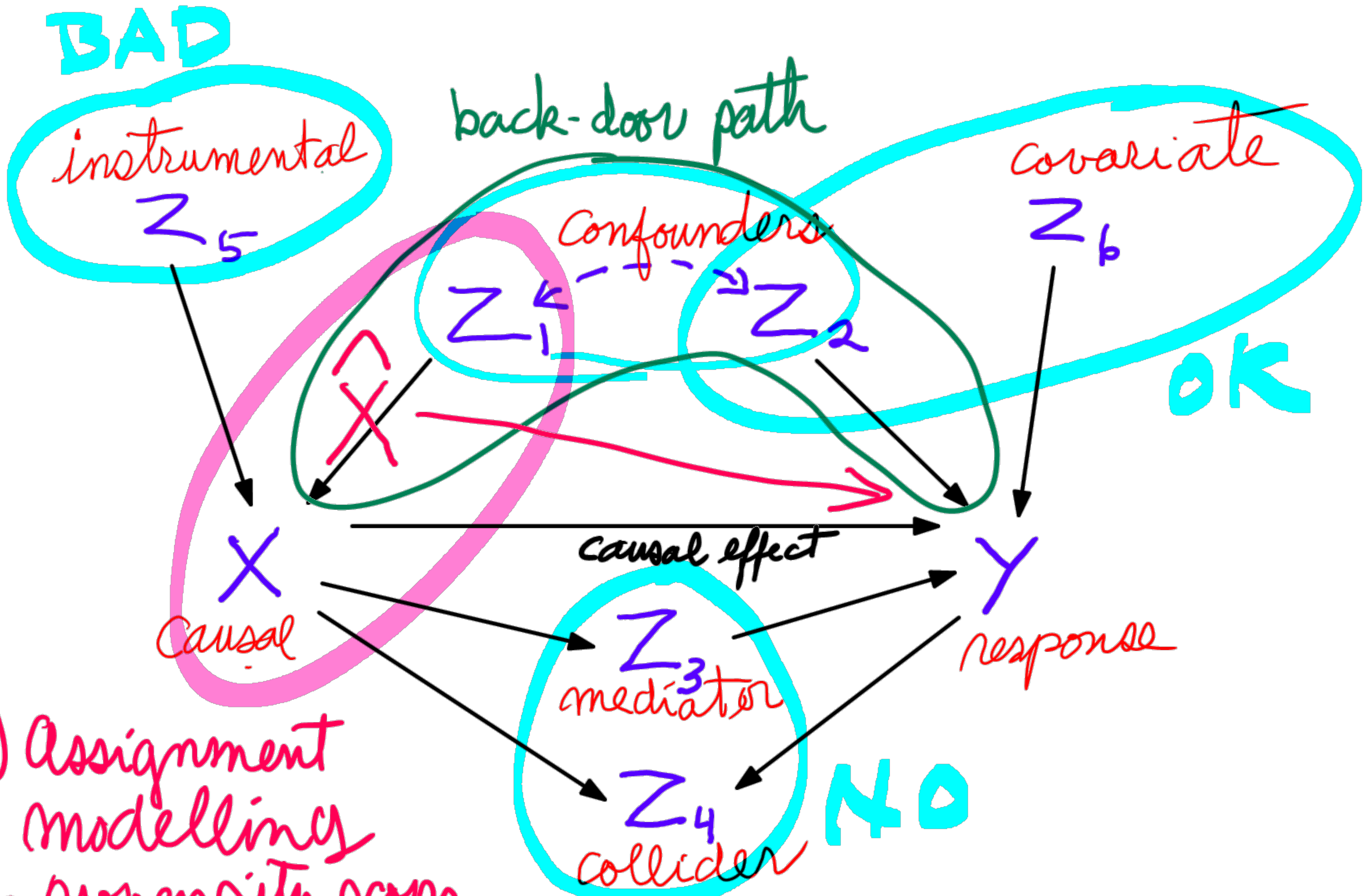

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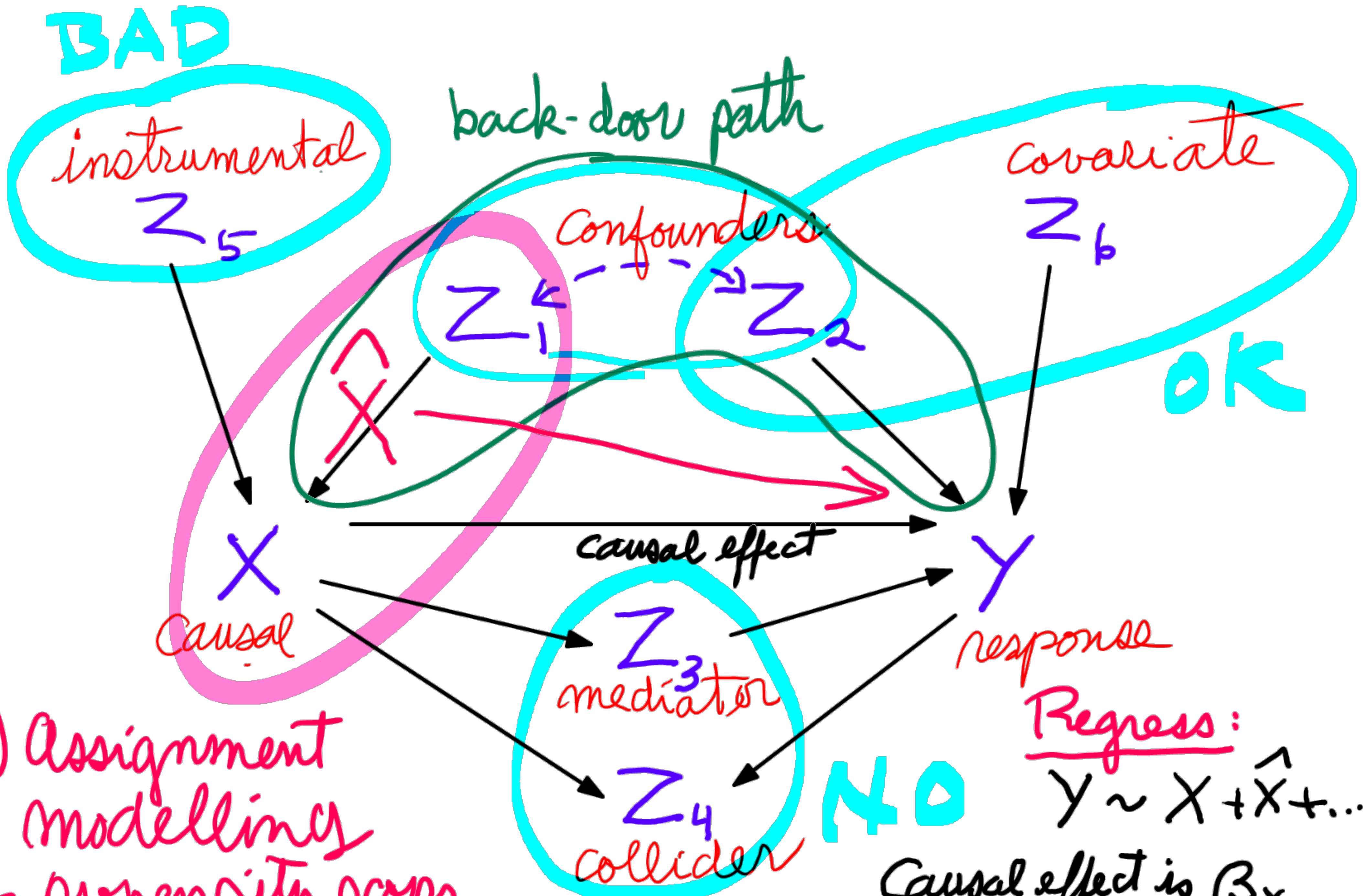
– propensity scores



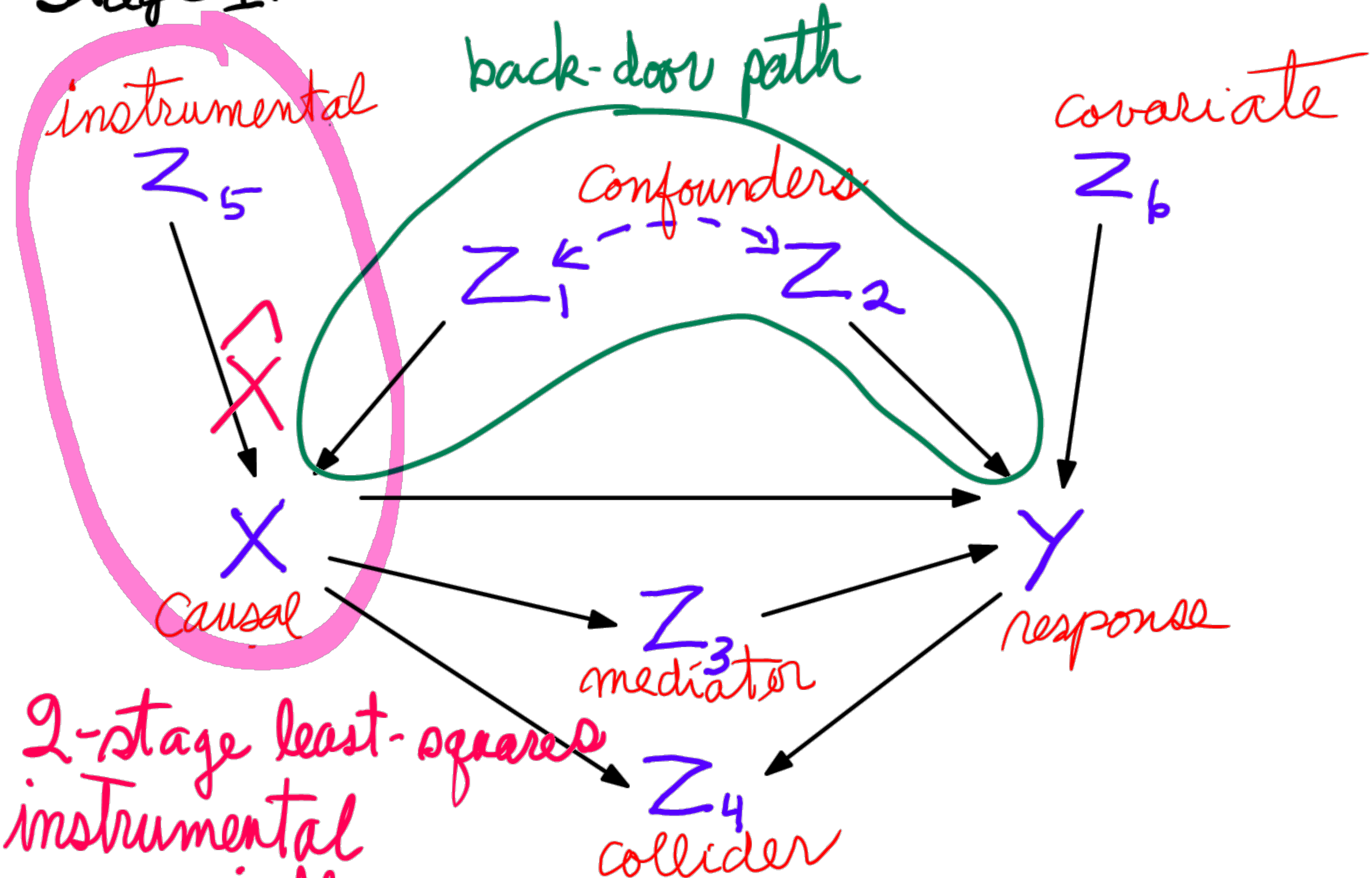
3) Assignment modelling
- propensity scores

<u>Regress:</u>

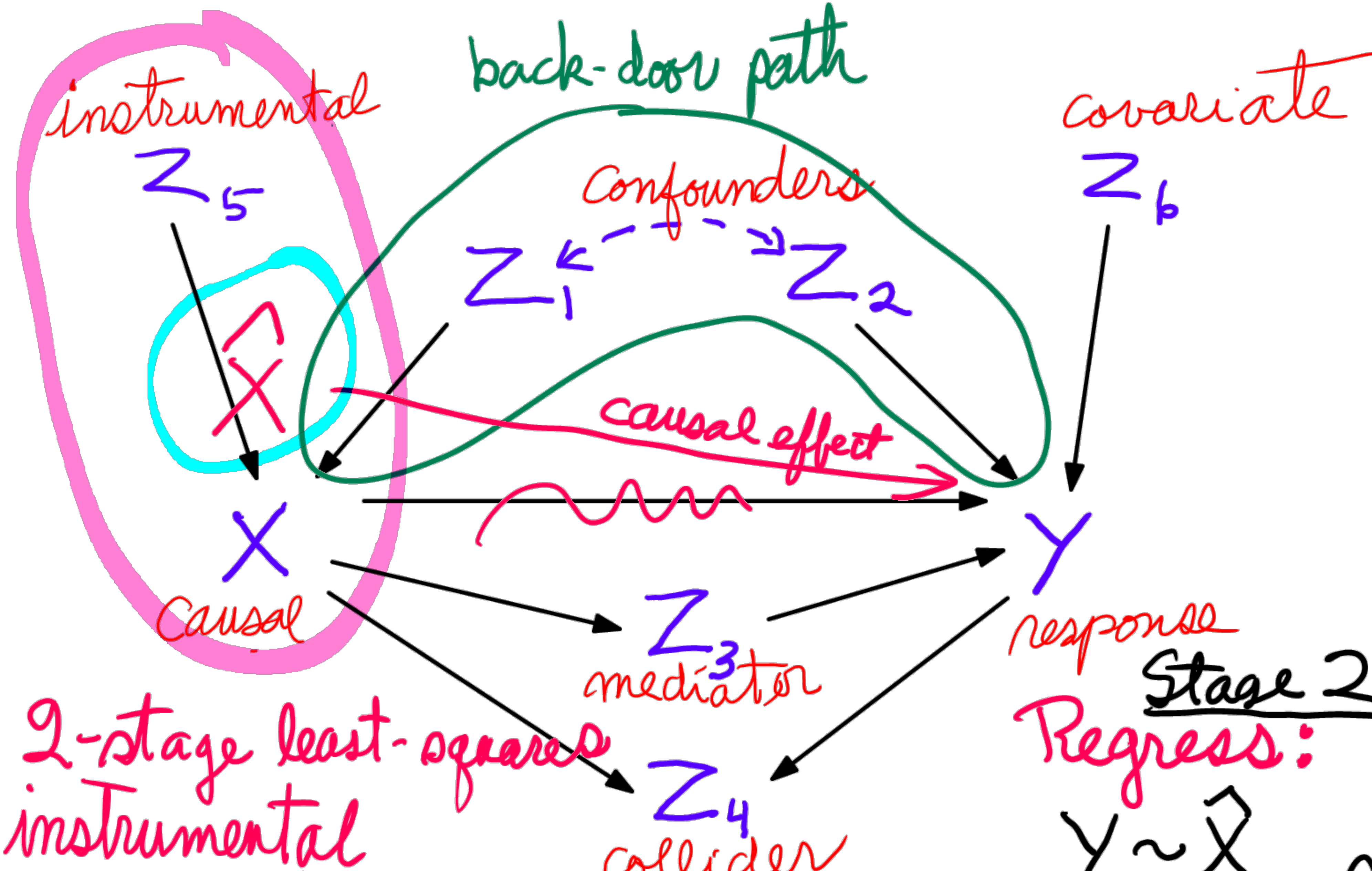
$Y \sim X + \hat{X} + \ldots$

Causal effect is β_X

Stage 1:



4) 2-stage least-squares instrumental variables



4) 2-stage least-squares
instrumental
variables

Stage 2

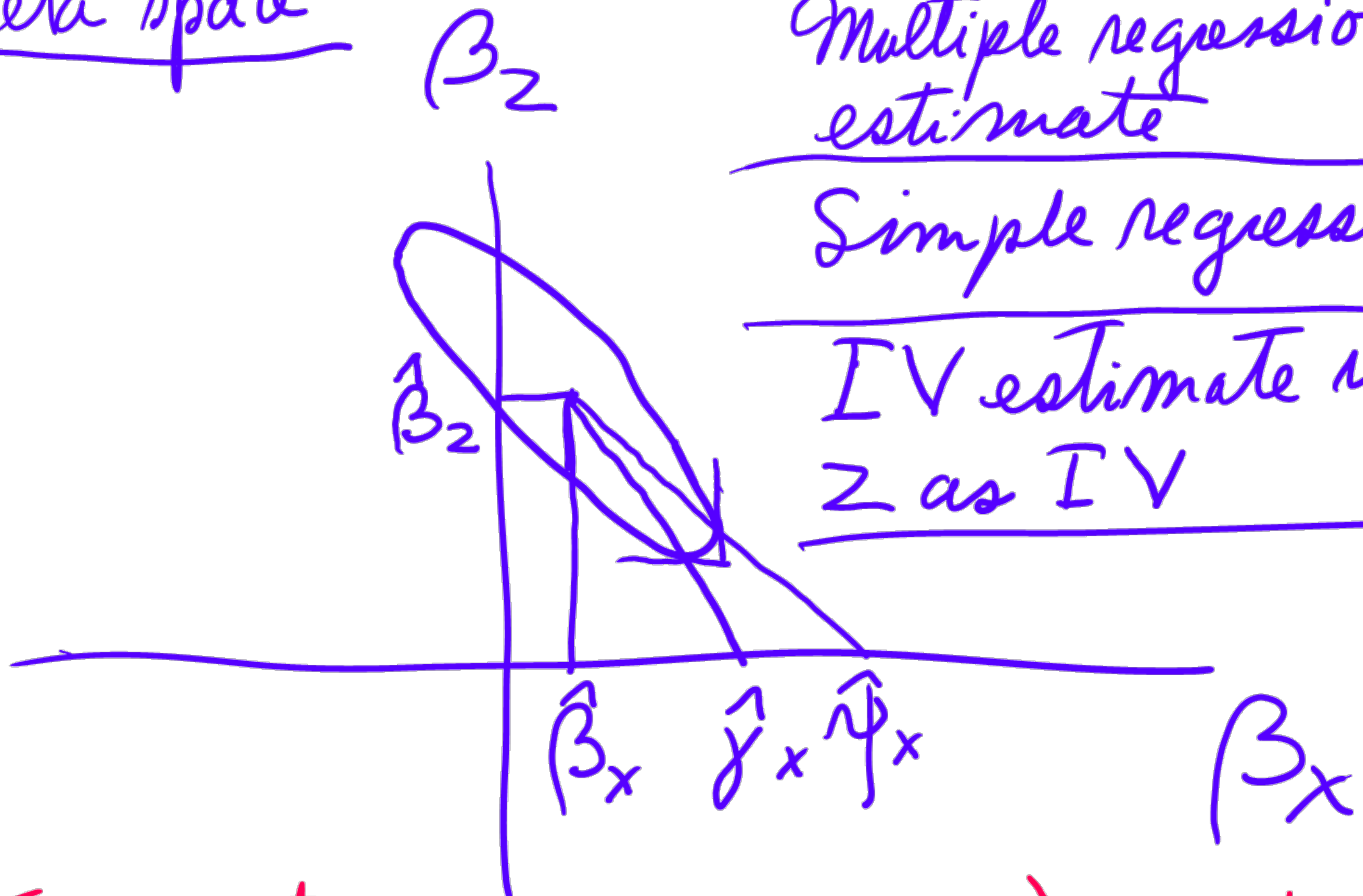
Regress:

$Y \sim \hat{X}$

Causal effect is $\beta_{\hat{X}}$

Beta space

Multiple regression estimate	$\hat{\beta}_x$
Simple regression	$\hat{\gamma}_x$
IV estimate with Z as IV	$\hat{\psi}_x$



For a strong IV, Corr(X, Z) close to 1 and exclusion restriction $\Rightarrow \beta_2$ close to 0

$\boxed{\text{So } \hat{\psi} \text{ close to } \hat{\gamma}_x}$

Note that we can't test the assumption of "exclusion restriction" by looking at the coefficient of the instrumental variable I in the regression

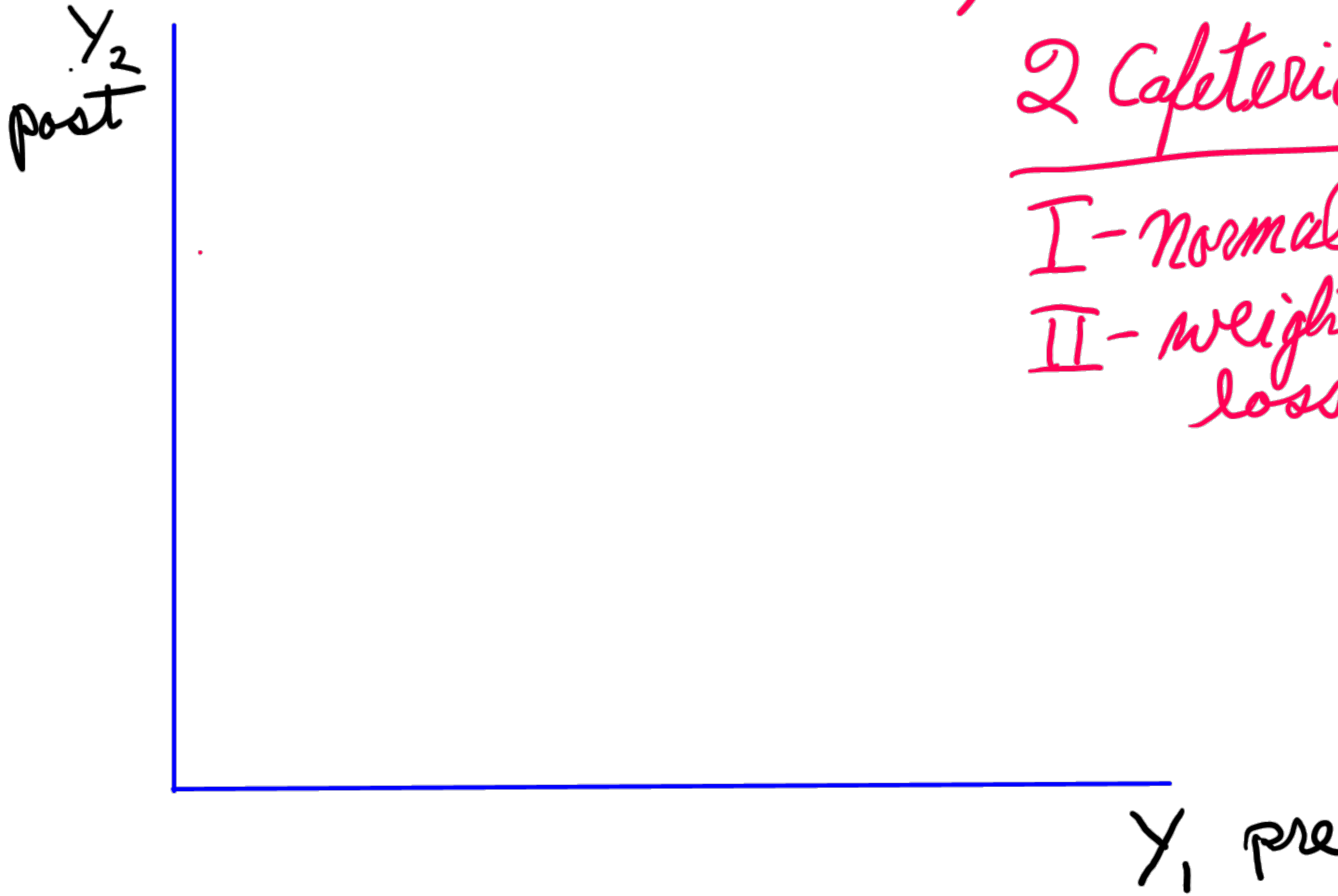
$$Y \sim I + X$$

since X is a collider if there is an omitted confounder C

$$\begin{tikzcd}
I \arrow[dr] & & C \arrow[dl] \arrow[dr] & \\
& X \arrow[rr] & & Y
\end{tikzcd}$$

and $\hat{\beta}_I$ should not be 0 even if I is a good instrument.

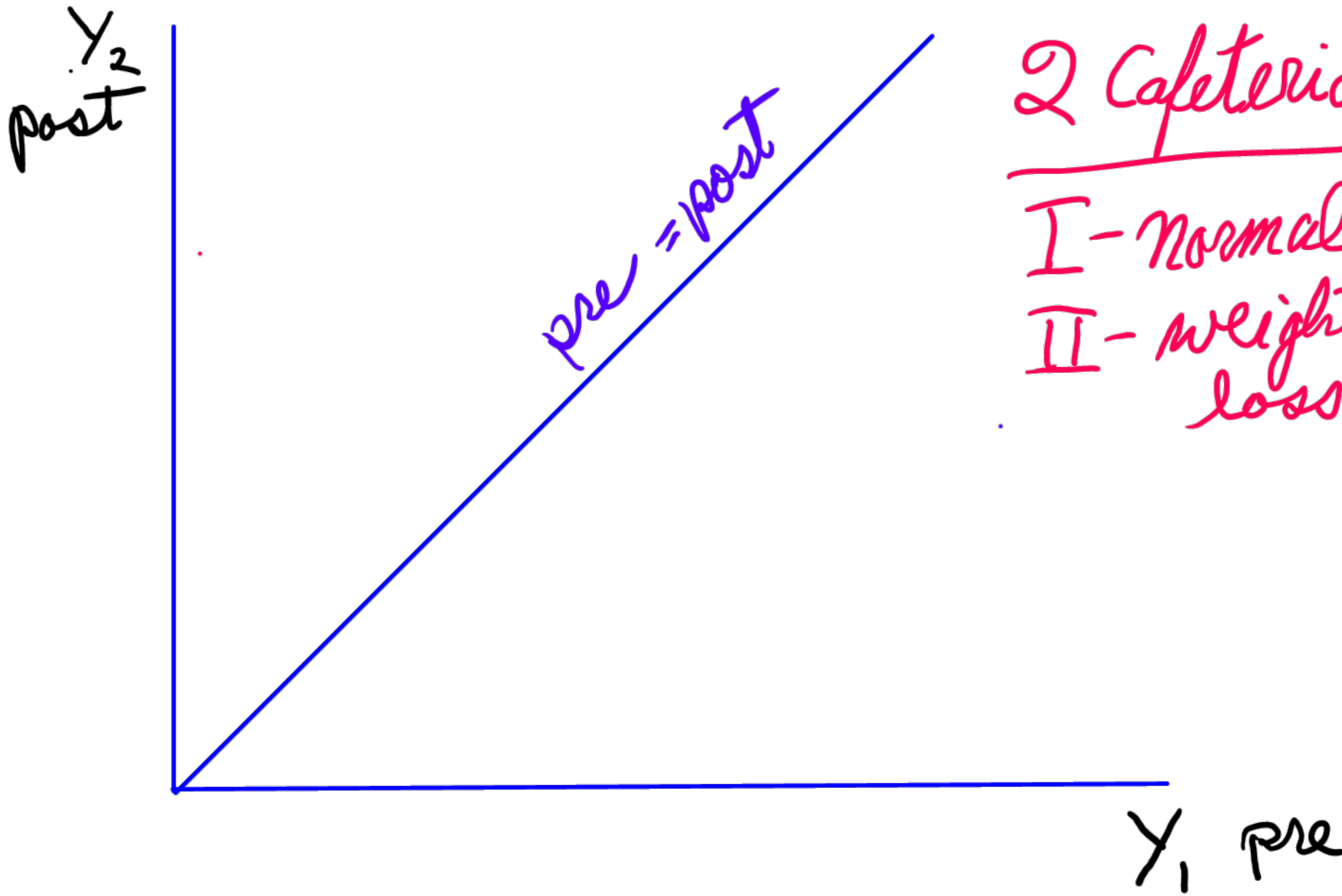
Lord's Paradox (Wainer version)



2 Cafeterias

I - normal

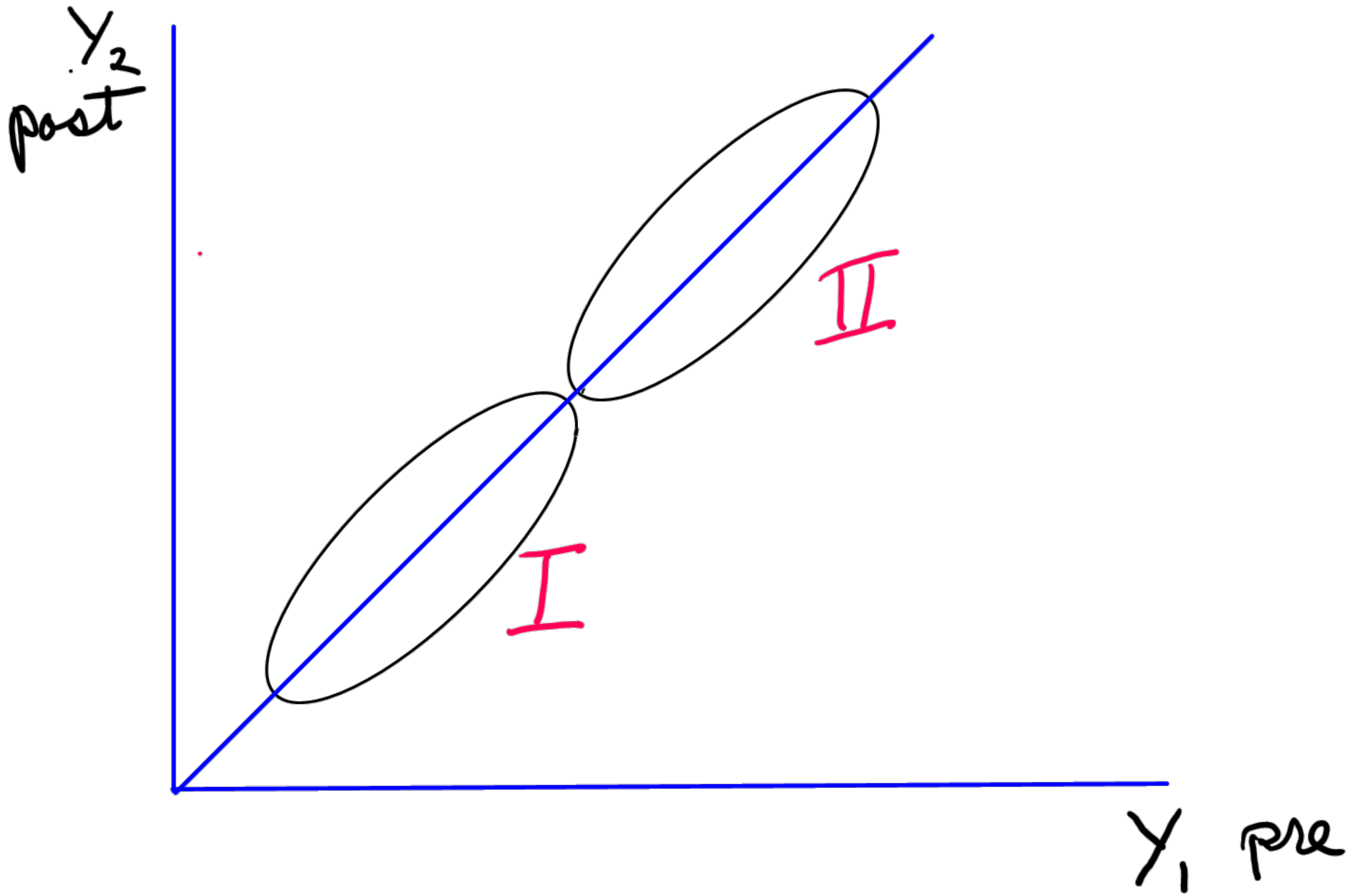
II - weight loss

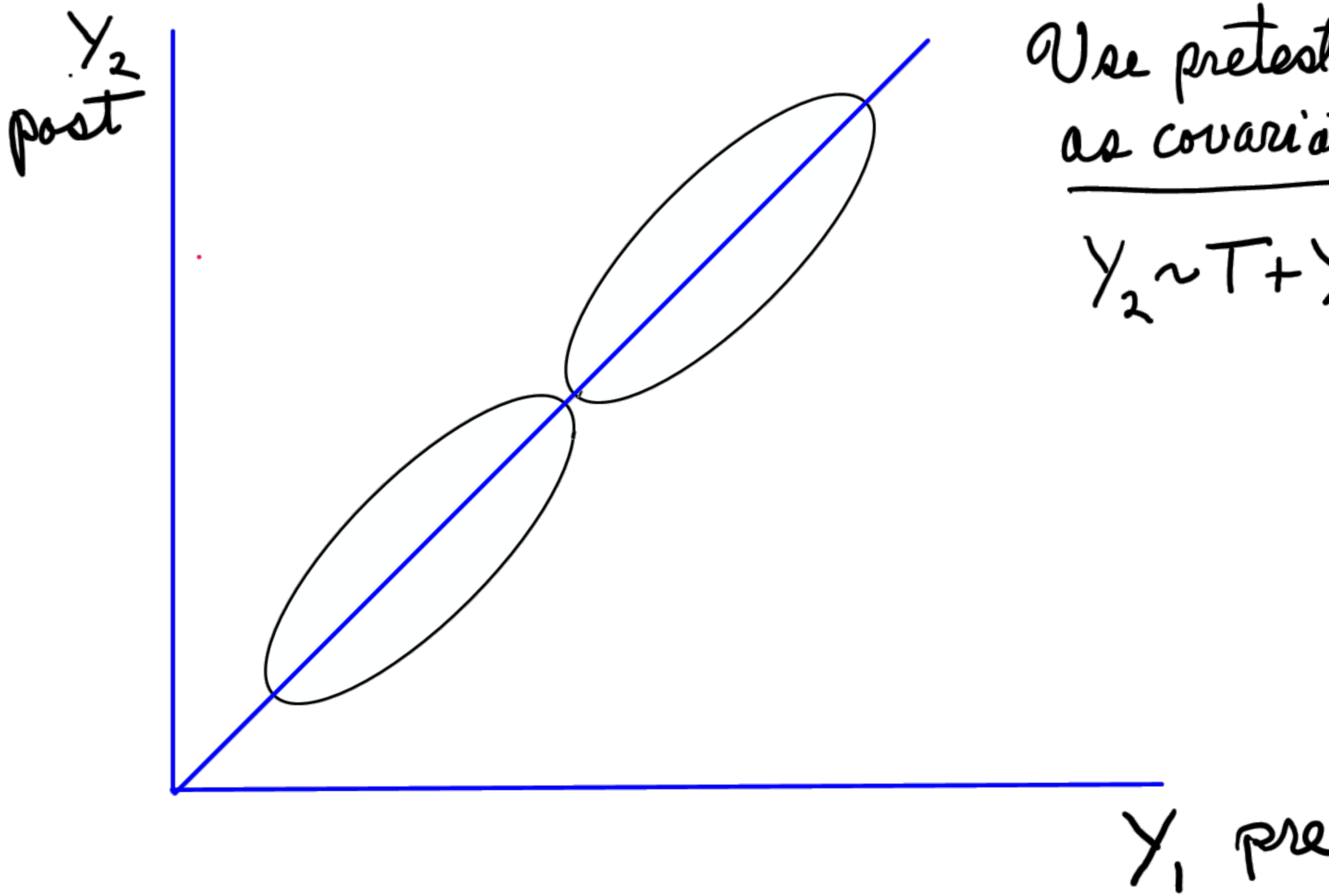


2 Cafeterias

I - normal

II - weight loss


Y_2
post
I
II
Y_1 pre

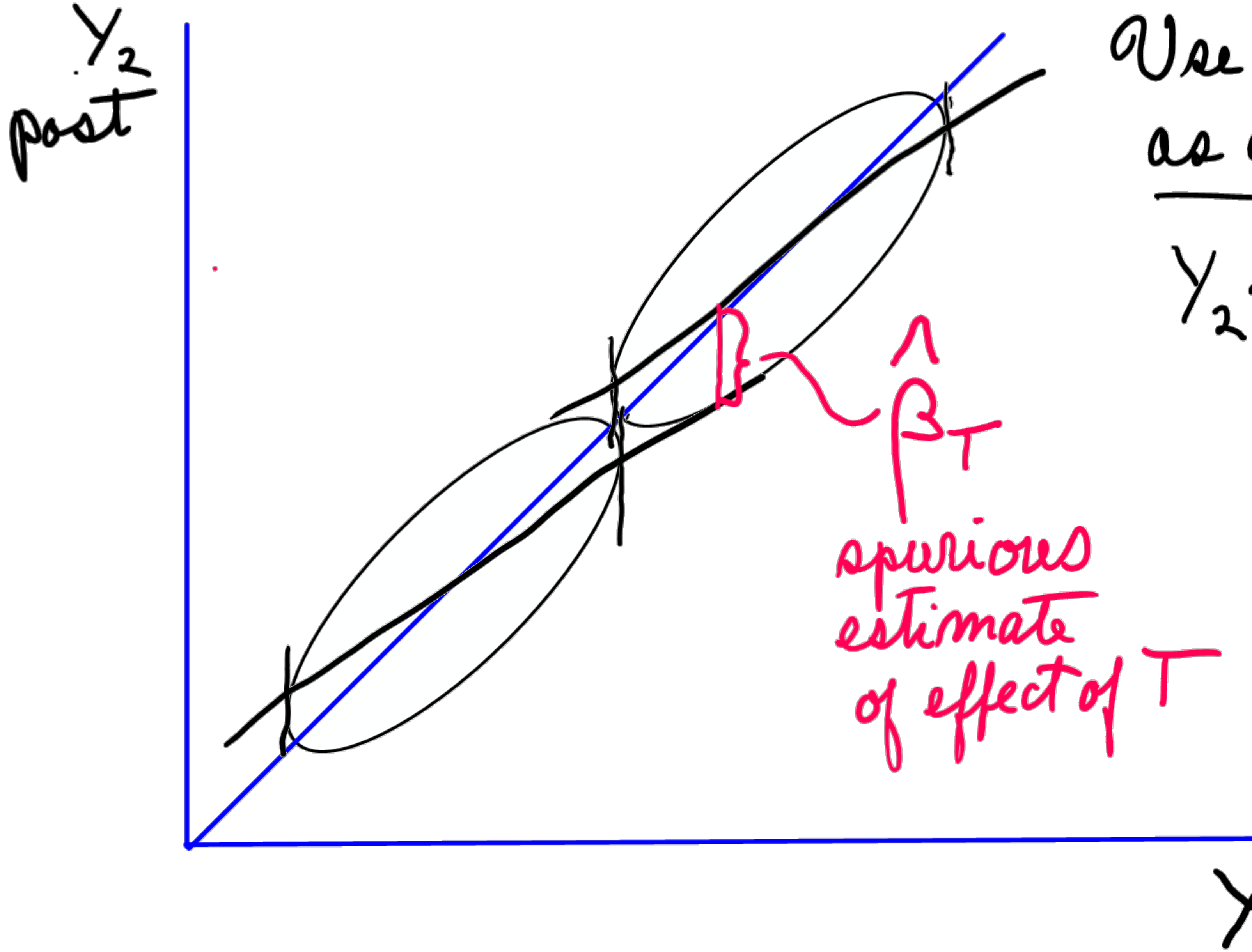


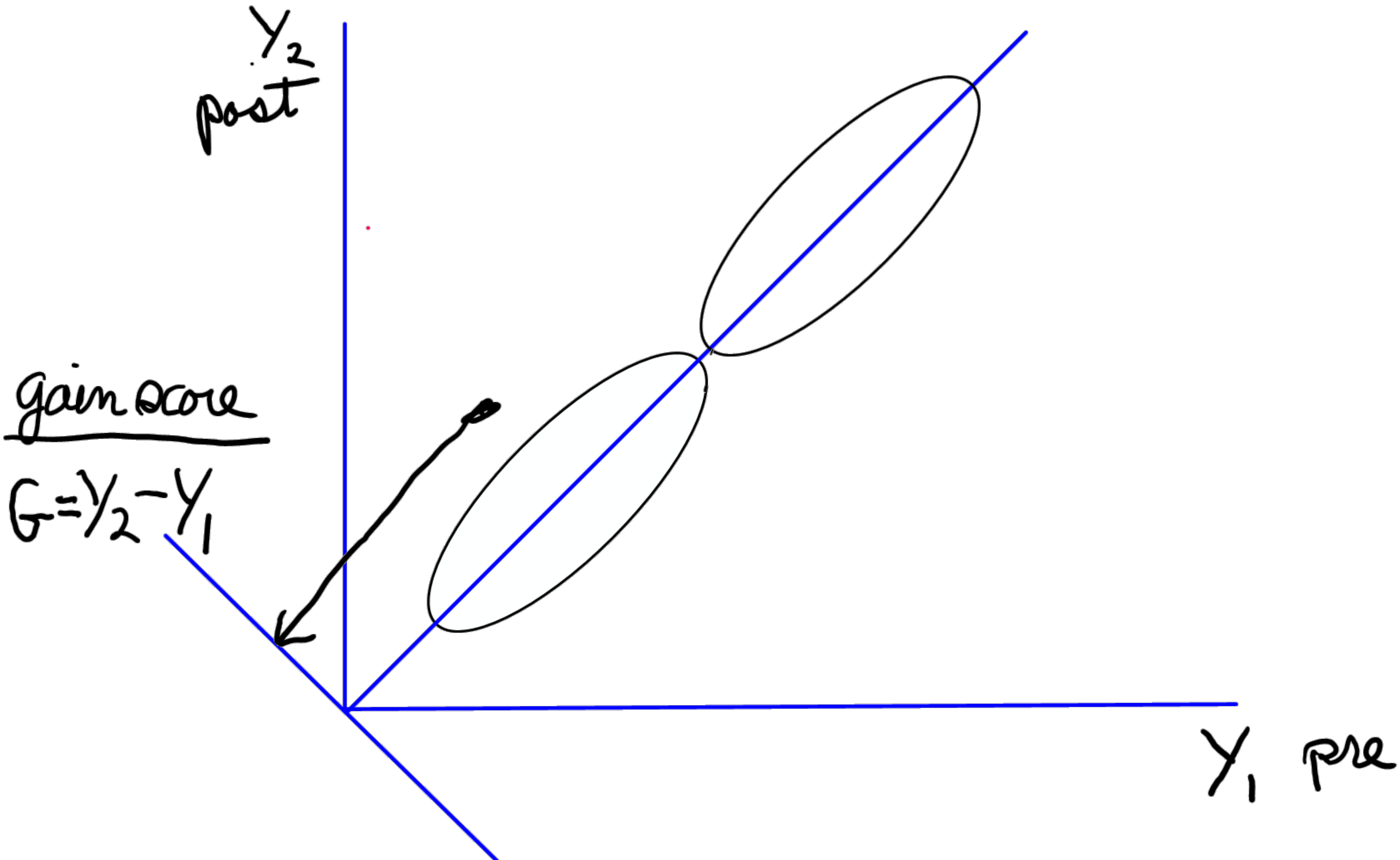
Use pretest as covariate

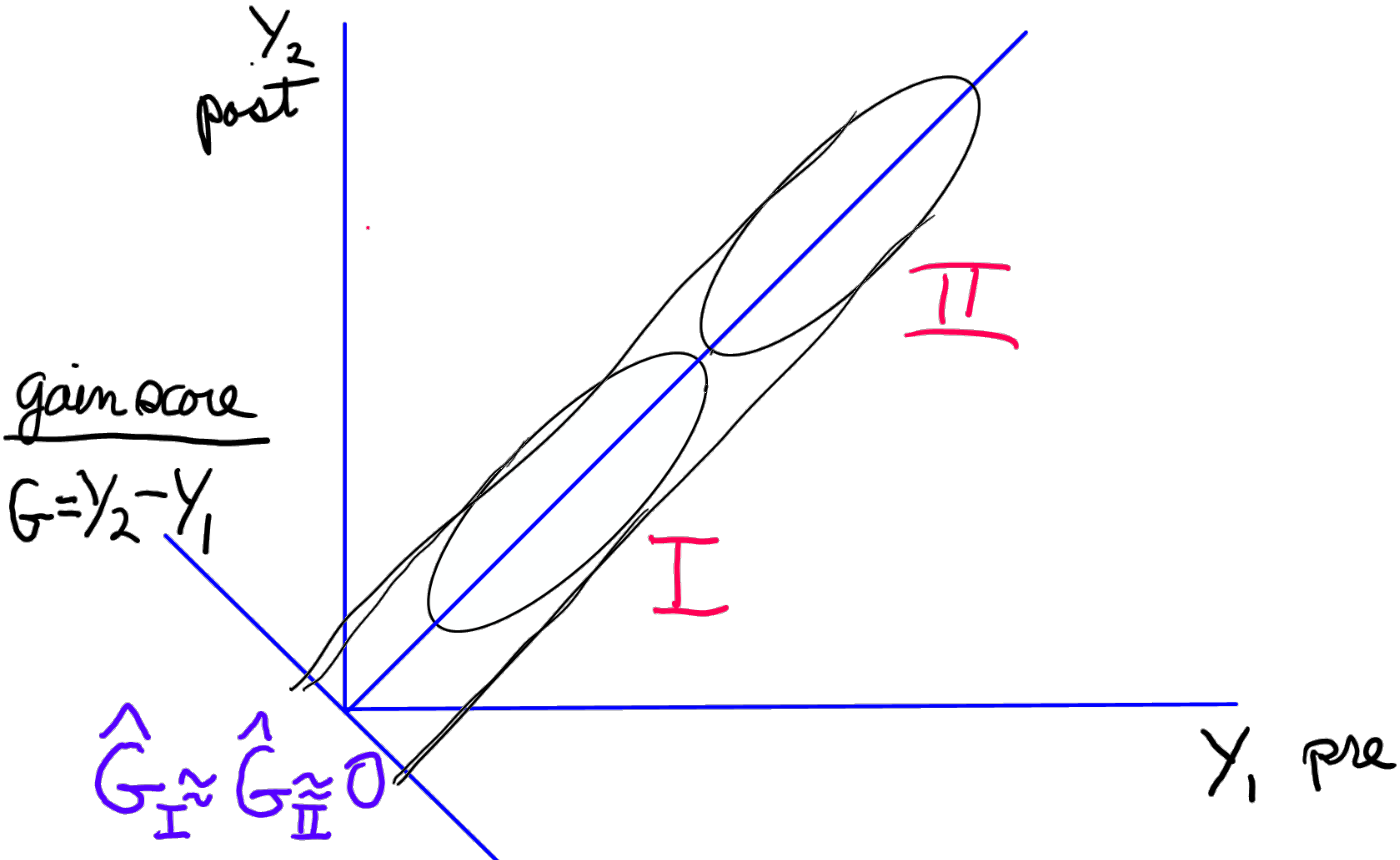
$Y_2 \sim T + Y_1$

Use pretest as covariate

$Y_2 \sim T + Y_1$

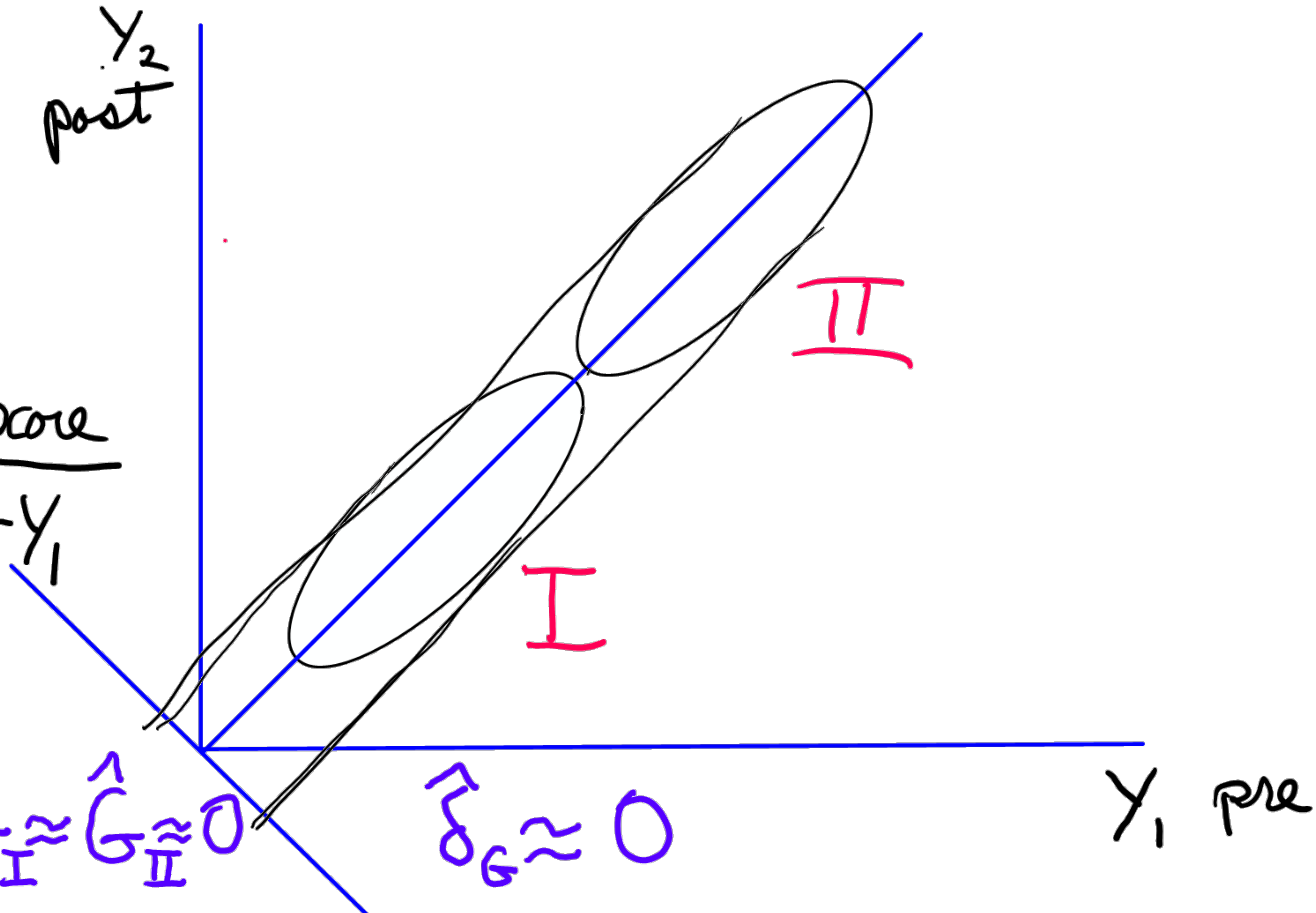



Y_2 post
gain score
$G = Y_2 - Y_1$
Y_1 pre

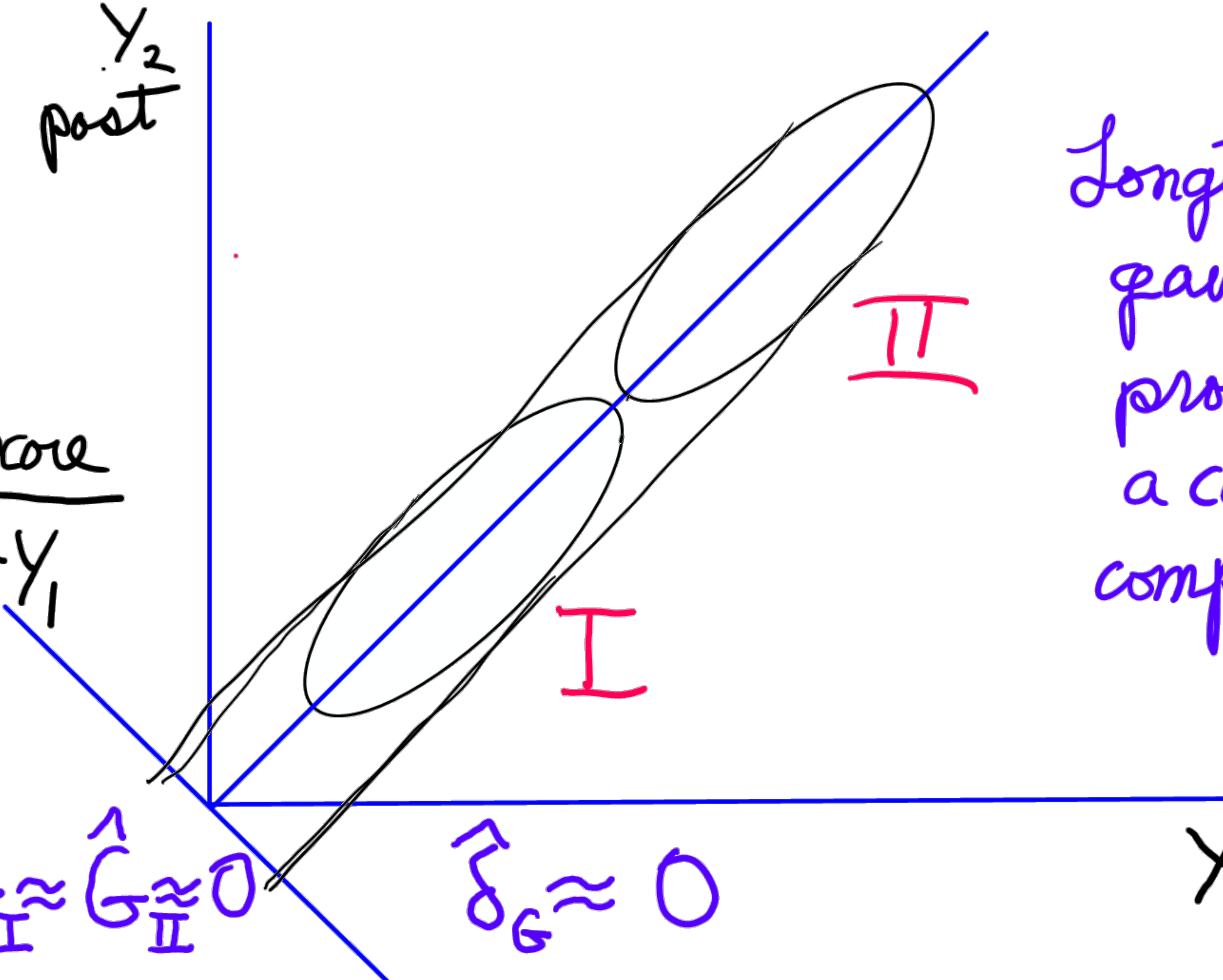

Y_2 post
gain score
$G = Y_2 - Y_1$
I
II
Y_1 pre
$\hat{G}_{I} \approx \hat{G}_{II} \approx 0$

gain score

$G = Y_2 - Y_1$



$\hat{G}_{I} \approx \hat{G}_{II} \approx 0$ $\hat{\delta}_G \approx 0$



gain score

$G = Y_2 - Y_1$

Longitudinal gain score provides a correct comparison

$\hat{G}_{I} \approx \hat{G}_{II} \approx 0 \quad \hat{\delta}_G \approx 0$

Conditions

- Same scale for Y_{pre} & Y_{post}
- No time-varying confounders

Within-subject effect adjusts for between-subject confounders whether measured or not.

Good model? $Y \sim X + Z_i + Z_j$

Want:

1) Unbiased : consistent

   Block back doors – NOT mediators & colliders

2) Low SE $= SD(Y_{res}) / SD(X_{res})$

   Small $SD(Y_{res})$, Large $SD(X_{res})$

3) Honest SE

4) Robust Propensity scores – focus on X

Use the AVP to compare models.

Using confounders close to Y

$\downarrow SD(Y_{res})$ and $\uparrow SD(X_{res})$ $\Rightarrow$ $\downarrow SE(\hat{\beta}_T)$

$$\left.\begin{array}{l}\downarrow SD(Y_{res})\\ \uparrow SD(X_{res})\end{array}\right\} \downarrow SE(\hat{\beta}_T)$$

But may not have knowledge about structure of model for Y

Using confounders close to X

$$\left.\begin{array}{l}\uparrow SD(Y_{res})\\ \downarrow SD(X_{res})\end{array}\right\} \uparrow SE(\hat{\beta}_T)$$

But may have better understanding of assignment model for X

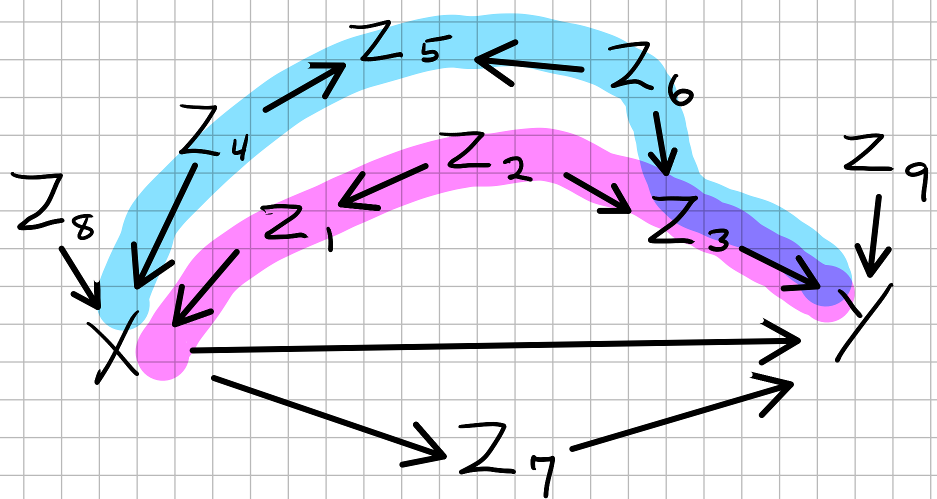
Propensity score methods focus on predicting X with $\hat{X}$

- no need to understand model for Y
- except to avoid mediators & colliders

Then regress Y on X and $\hat{X}$ (often grouped into intervals)

"Doubly robust:" throw in some Z's close to Y and covariates.

Summary for linear models:



Back door path #1

" " " #2

- Not including Z_5 blocks #1
- Any of Z_1, Z_2, Z_3 blocks #2

Will $Y \sim X + X_i + X_j$ estimate the causal effect of X?

2 requirements that are sufficient

1) Block back-door paths
   How?
   a) Presence of a collider NOT in the model
   OR
   b) Including one or more non-colliders
2) Do not include descendants of X

$SD(\hat{\beta}_X) = ? = \frac{1}{\sqrt{n}} \frac{S_e}{S_{X|others}}$

Comparing models, consider impact on S_e & $S_{X|others}$

gation

age

3:42

Fascism makes MOST DIRE WARNING about Trump Yet | Burn The Boats

uch