Solutions

York University MATH 4939 – Midterm

Instructor: Georges Monette

February 14, 2020 – 9:30 am to 10:20 am (50 minutes)

WARNING

DO NOT OPEN THIS BOOKLET UNTIL YOU ARE INSTRUCTED TO DO SO

Student number:	
Family name: (in BLOCK letters)	
Given name: (in BLOCK letters)	
Signature	

Information:

Be sure to read questions closely. Some may ask for multiple pieces of information. Make sure to respond completely. If you need more space to answer, write "**OVER**" and continue the answer on the back of the page.

The marks for each questions are shown at the end of the question. The sum of the marks is 105. The exam will be graded out of 100 so that you can potentially earn 5 bonus points.

 ${\bf Aids\ allowed:}\ {\bf Non\text{-}programmable\ calculator},\ {\bf ruler},\ {\bf pencils},\ {\bf pens},\ {\bf erasers}.$

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1. In R, the data frame mtcars has 32 rows and 11 variables of which cyl is a variable recording the number of cylinders in each type of car. Fix each of the following common data frame subsetting errors in R:

(20 points)

2. The following is some output from a linear regression of life expectancy in a number of countries regressed on HE (health expenditures per capita per year in dollars US), smoke (cigarettes per capita per year), hiv and special, that are two indicator variable to identify anomalous countries.

```
Call:
lm(formula = LifeExp \sim log(HE) * (smoke + I(smoke^2)) + hiv +
    special, data = dd, na.action = na.exclude)
Residuals:
   Min
             10 Median
                             3Q
                                    Max
-9.0373 -2.3005 0.2043 2.0760
                                9.7344
Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
(Intercept)
                    3.283e+01 2.674e+00 12.280 < 2e-16 ***
log(HE)
                    6.091e+00 5.024e-01 12.124 < 2e-16 ***
                    3.642e-02 7.520e-03 4.844 3.31e-06 ***
smoke
I(smoke^2)
                   -1.518e-05 3.946e-06 -3.846 0.000181
hiv
                   -7.351e-01 7.593e-02
                                         -9.681 < 2e-16
                                         -8.526 2.11e-14 ***
special
                   -1.822e+01 2.137e+00
                   -4.878e-03 1.155e-03 -4.223 4.30e-05 ***
log(HE):smoke
log(HE):I(smoke^2)
                   2.007e-06
                                           3.504 0.000614 ***
                               5.726e-07
```

Construct a hypothesis matrix to estimate the predicted difference in life expectancy associated with an increase of 1,000 cigarettes per capita per year for a country with a level of health expenditures equal to 2,000 and cigarette consumption equal to 1,000.

```
2,000 and cigarette consumption equal to 1,000.

*(10 points)* Since the not linear in 'smohe' we need to
take a difference

Lea HE = 2000 & Smoke = 1000:

[1 log 2000 1000 1000 hiv special log 2000 1000 log 2000 1000<sup>2</sup>]

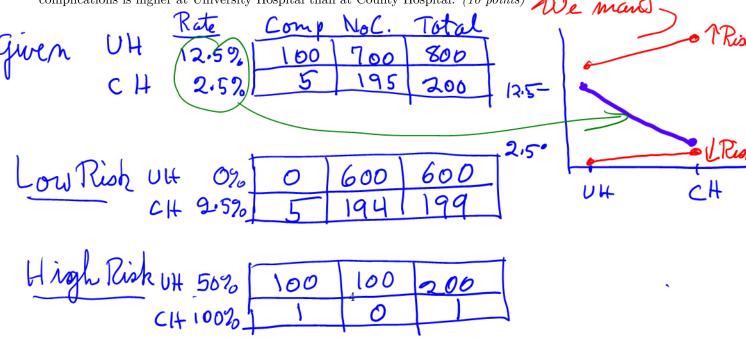
Lea HE = 2000, Smoke = 2000:

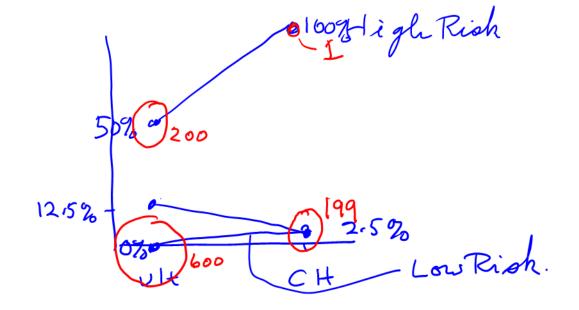
[1 log 2000 2000 2000 hiv special log 2000 2000 log 2000 2000]

[1 log 2000 2000 2000 0 0 log 2000 2000 log 2000 3000000]
```

3. (continued from the previous question) Construct a hypothesis matrix to estimate the predicted difference in life expectancy associated with an increase of 1,000 dollars in health expenditures per capita per year for a country with a level of health expenditures equal to 2,000 and cigarette consumption equal to 1,000. (10 points)

4. Here are some fictitious data on the rate of complications for appendectomies performed at University Hospital, a large urban teaching and research hospital, and in County Hospital, a small-town hospital: at University Hospital there were 800 cases with 100 (12.5%) resulting in complication and at County Hospital there were 200 cases resulting in 5 (10%) complications. The p-value for a test of the hypothesis that there is no difference in the rate at the two hospitals is 0.0037. Suppose that appendectomies can be classified as high risk or low risk and that the high risk cases tend to be directed disproportionately to University Hospital instead of County Hospital. Construct two hypothetical tables, one for each level of risk, and draw a Paik diagram that shows how it is possible for both high- and low-risk patients to have a lower probability of complications at University Hospital than at County Hospital, although, overall the probability of complications is higher at University Hospital than at County Hospital. (10 points)





5. Suppose a test for glaucoma has a sensitivity of .95 and a specificity of .90. You receive the test as a routine test on a regular visit to your optometrist. The prevalence of glaucoma in your age, ethnic and gender group among people who have not been previously diagnosed is 1 per 100. The test, alas, is positive. Use a natural frequency table to find the probability that you have glaucoma given the positive test result. (10 points)

6. Suppose you were to read about a study based on a random survey of Ontario medical records that shows that smokers have twice as high a risk of kidney disease as non-smokers. Is it reasonable to conclude that smoking causes a higher risk of kidney disease? Why or why not? (10 points)

no because

a) Treatment clearly not randomized since it's a random survey of records so we can trely on random assignment to infer a cansal effect of smoking.

b) The rish comparison compares all smoters with all non smoters so there is no control for

possible confounding factors, which would need to be controlled for to justify the inference of a Causal relationship.

7. When performing a regression, discuss situations when a) it would be important to include a variable that is not significant and b) it would be important to exclude a variable that is highly significant. Give examples of each situation. (15 points)

the regression is performed for Causal inference with observational data, it is important a) block confounding back-door atho by controlling for some confounding factors along each path even if the varible so not significant b) Omit mediating factors even - Particularly if- a factor is Dignifo Of 1 stress causes 11 coffee consumption and an in heart damage Then the Confounding effect need be controlled to causal effect of coffee.

Of T coffee consumption causes heart damage by increasing some hormone, say adrenalin, whose higher levels in turn cause heart damage, then it is important to omit adrenalin levels in a segression to estimate the causal effect of coffee.

```
d1 <- data.frame(id = c('a', 'a', 'b', 'c'), grade = c(1, 2, 1, 3))
d2 <- data.frame(id = c('a', 'c', 'c', 'd'), year = c(3, 1, 3, 4))
Describe the differences between the outputs of the following commands:
a. merge(d1, d2)
b. merge(d1, d2, all.x = TRUE) (10 points)
```

Since id so the only wariable in both dI and d2, it is the key variable that links the two data frames for mereging. The command in (a) take every combination for levels of "id" that occur in both d1 & d2
The result of (a) is:

id grade year

a 1 3
a 2 3
C 3

The result of (b) takes every
row of d! whether matched in d?
or not a On addition to the
rows above the result also
includes
indudes
id grade year

9. Write a function in R that takes a character string and collapses multiple adjoining blanks between words to a single blank and remove leading and trailing blanks. (10 points)

 \mathbf{END}