# Mediators Confounders and Colliders, oh my!

Christina T Saunders, PhD Department of Biostatistics

# Goals for understanding

Use causal diagrams to understand:

What is a **mediator**?

What is a **confounder**?

What is a **collider**?

Use causal diagrams and domain expert knowledge to answer:

Which variables should we condition on in a regression model?



"When we draw an arrow from X to Y, we are implicitly saying some probability rule or function specifies how Y would change if X were to change." Pearl 2018



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A back-door path is any path from X to Y that starts with an arrow pointing into X.



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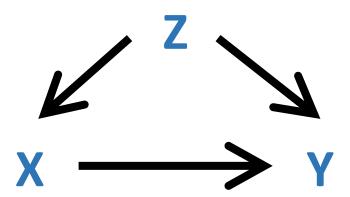
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No backdoor path

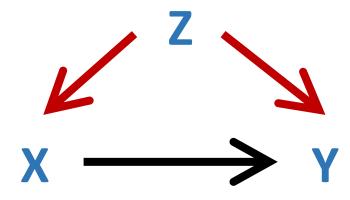
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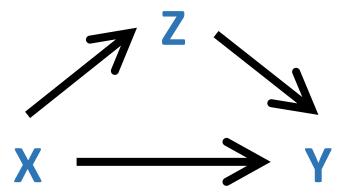
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Backdoor path from  $X \leftarrow Z \rightarrow Y$ 

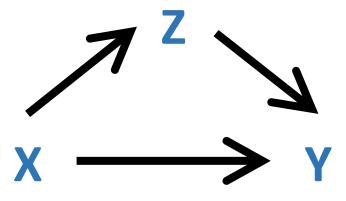
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No backdoor path

Data shows increased ice cream sales are associated with more crime... Ice cream sales cause crime?



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But our brains say that doesn't make any sense!



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Solution: Condition on "background factors" (aka confounders) K.

# **VERY IMPORTANT QUESTION:**

Which variables should we condition on?

#### 3 kinds of *junctions*

1. Chain:  $A \rightarrow B \rightarrow C$ 

2. Fork:  $A \leftarrow B \rightarrow C$ 

3. Collider:  $A \rightarrow B \leftarrow C$ 



1. Chain:  $A \rightarrow B \rightarrow C$ 

#### 1. Chain: A $\rightarrow$ B $\rightarrow$ C

B is the mechanism or mediator that transmits the effect of A to C.

Fire ♦ → Smoke → Alarm

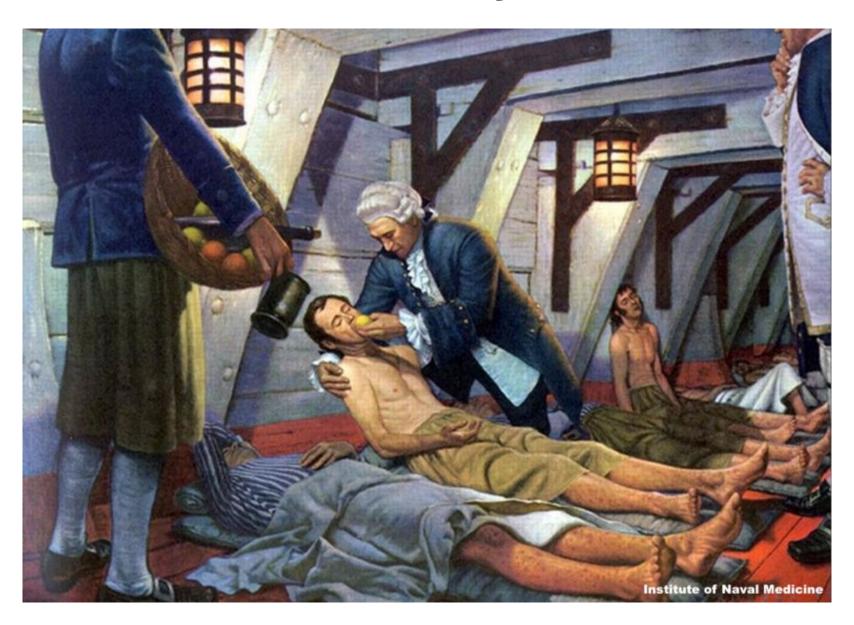
Fire only causes the alarm to go off via producing smoke. There is no direct arrow from Fire  $\rightarrow$  Alarm.

Controlling for B (mediator) prevents information about A (exposure) from getting to C (outcome), and vice versa.

# Why do a mediation analysis?

To understand causal mechanisms and to answer questions like "How?" and "Why?"

# Scurvy



#### Dr. James Lind credited with the first clinical trial in 1747

#### Administered 6 different treatments to 12 afflicted sailors:

- 2 spoons of vinegar
- 1 quart of cider
- 1 cup of seawater
- 2 oranges, 1 lemon
- 25 drops elixir of vitriol
- Paste of garlic, mustard seed, horseradish

Sailors who were given the citrus fruits got better.

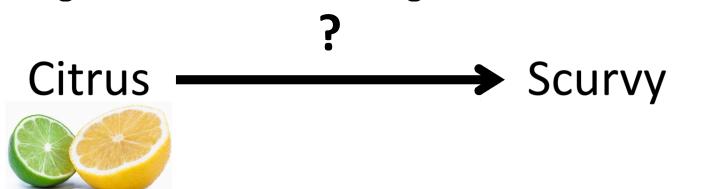


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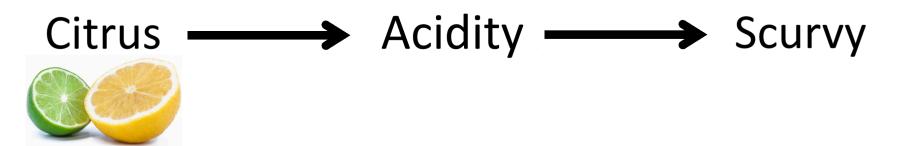
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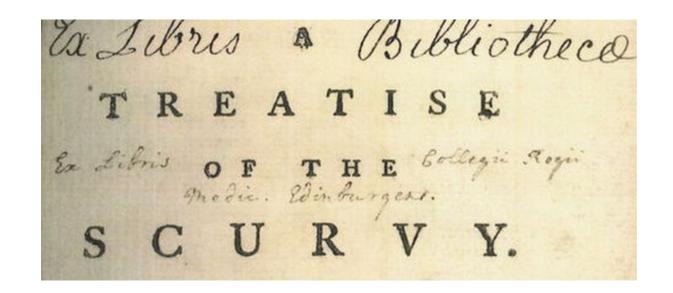
Sailors who were given the citrus fruits got better. BUT WHY?



#### Lind suggested lemons worked due to their acidity

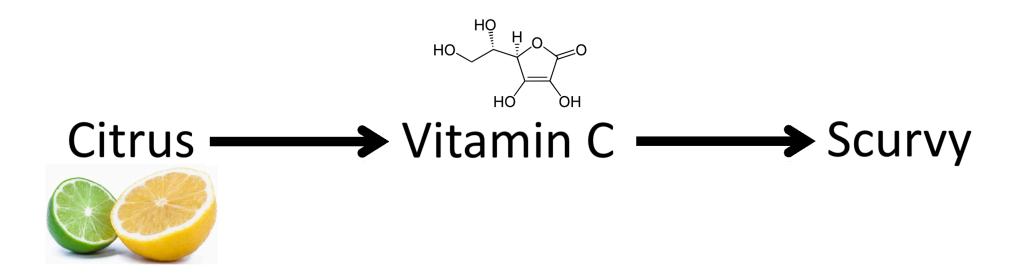
Published *Treatise of the Scurvy* in 1753





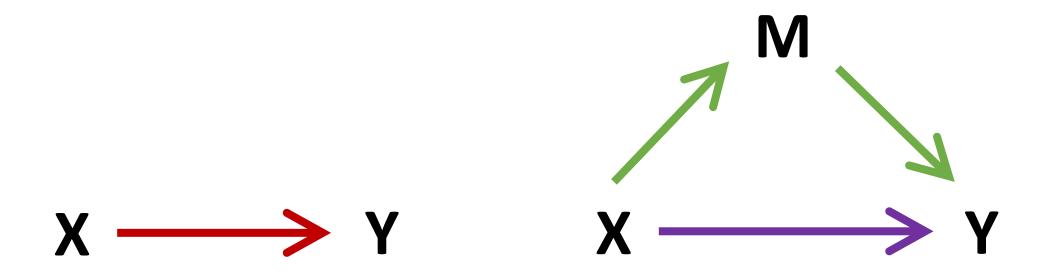
#### Vitamin C discovered by Albert Szent-Gyorgyi in 1933

Feeding the sailors citrus fruits increased their vitamin C levels, which in turn remedied their scurvy



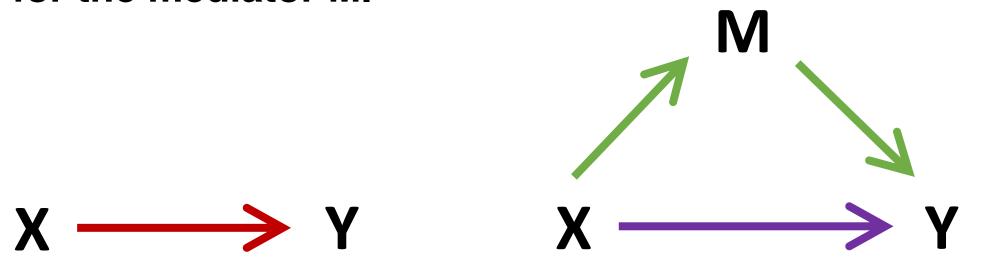
Vitamin C is a mediator of the effect of citrus on scurvy

Mediation Analysis decomposes the total effect of exposure X on outcome Y into the direct effect and the mediated effect transmitted through M.



To estimate the total effect of X on Y, DO NOT adjust for the mediator M.

To estimate the the direct effect of X on Y, DO adjust for the mediator M.



2. Fork:  $A \leftarrow B \rightarrow C$ 

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Confounder makes A and C statistically correlated even though there is no direct causal link between A and C.

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Confounder makes A and C statistically correlated even though there is no direct causal link between A and C.

Shoe size **९ ←** Age of child → Reading ability **९** 

Children with larger shoes tend to read at a higher level. But giving a child larger shoes won't make him read better...

Controlling for B (confounder) prevents information about A (exposure) from getting to C (outcome), and vice versa.

### **Confounder Example:**

1996 observational study data comparing endoscopic vs open surgery showed:

- Higher probability of successful removal of small kidney stones using open surgery
- Higher probability of successful removal of large kidney stones using open surgery
- Higher probability of successful removal of kidney stones using endoscopic surgery

### **Confounder Example:**

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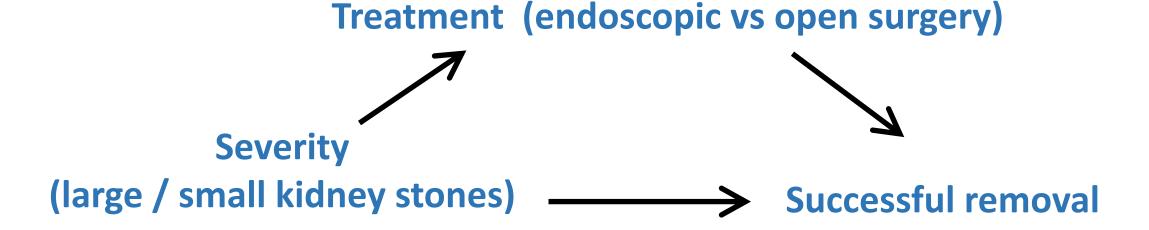
Open surgery is better for small and large kidney stones, but worse for all kidney stones?



### **Confounder Example:**

Kidney Stone Severity is a confounder of Treatment and Successful Removal.

To obtain unbiased estimates of Treatment's effect on Success, we need to adjust for kidney stone severity. In this case, one should report the adjusted estimates.



3. Collider:  $A \rightarrow B \leftarrow C$ 

#### 3. Collider: $A \rightarrow B \leftarrow C$

B is a common effect or collider of A and C.

Conditioning on collider B *creates a dependence* between A and C even though they are unrelated in the general population. (collider bias is also known as <u>selection bias</u>)

We should not condition on colliders.

## **Collider Example: Smoking birthweight paradox**

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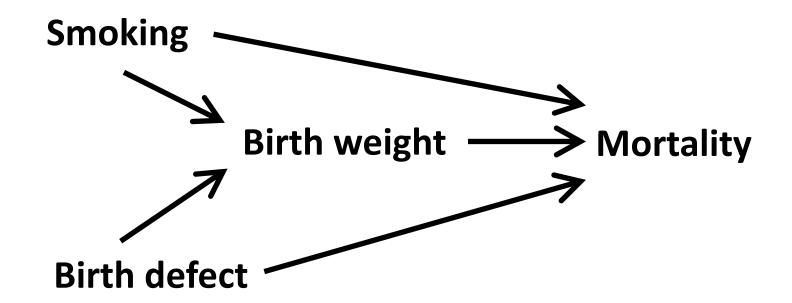
Prior studies have shown evidence of Smoking mother ⚠ → Low birthweight • → Mortality

Mid 1960s study by Yerushalmy on 15,000 children found that low birthweight babies of smoking mothers had *better survival* than low birthweight babies of nonsmoking mothers.

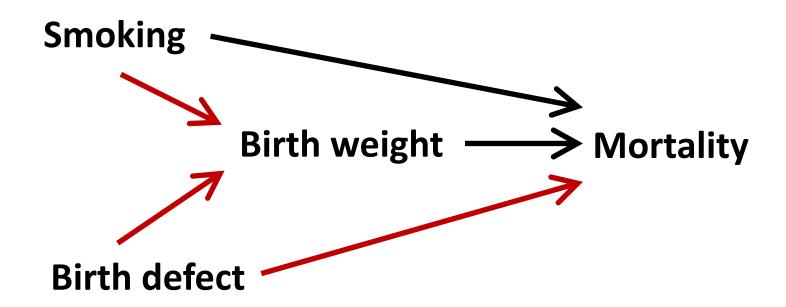
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Mid 1960s study by Yerushalmy on 15,000 children found that low birthweight babies of smoking mothers had *better survival* than low birthweight babies of nonsmoking mothers.

Mothers' smoking is protective? That doesn't make sense!



Birth weight is a collider!



When we look only at low birthweight babies (conditioning on a collider), we open a backdoor path from Smoking  $\rightarrow$  Birth weight  $\leftarrow$  Birth defect  $\rightarrow$  Mortality.

Stumped epidemiologists for decades!

"In this case, the collider bias was detected because the apparent phenomenon was too implausible, but just imagine how many cases of collider bias go undetected because the bias does not conflict with theory."

# Returning to our very important question: Which variables should we condition on?

#### To estimate the total effect of exposure X on outcome Y:

DO adjust for confounders (common causes of X and Y)

DO NOT adjust for colliders (common effects of X and Y)

DO NOT adjust for mediators (variables on the causal pathway)\*

# Returning to our very important question: Which variables should we condition on?

#### To estimate the total effect of exposure X on outcome Y:

DO adjust for confounders (common causes of X and Y)

DO NOT adjust for colliders (common effects of X and Y)

DO NOT adjust for mediators (variables on the causal pathway)\*

\* In a mediation analysis, you DO adjust for the mediator to estimate the *direct effect* of X on Y adjusted for M.

# Games from "Toward a Clearer Definition of Confounding" by Clarice Weinburg (a deputy chief at NIH)



American Journal of Epidemiology
Published by Oxford University Press on behalf of the Johns Hopkins Bloomberg School of Public Health 2012.

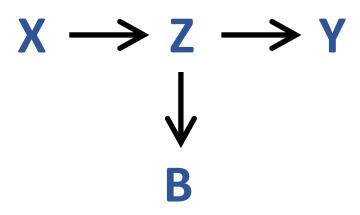
Vol. 176, No. 6 DOI: 10.1093/aje/kws127 Advance Access publication: August 17, 2012

#### Practice of Epidemiology

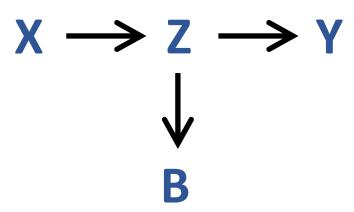
"Toward a Clearer Definition of Confounding" Revisited With Directed Acyclic Graphs

Penelope P. Howards\*, Enrique F. Schisterman, Charles Poole, Jay S. Kaufman, and Clarice R. Weinberg

#### Game 1:

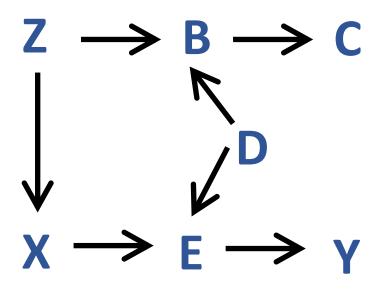


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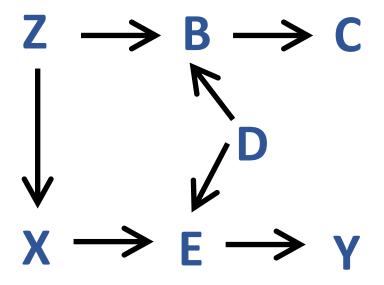


There are no back-door paths from X to Y (no arrows coming into X), so we don't need to control for anything.

#### Game 2:

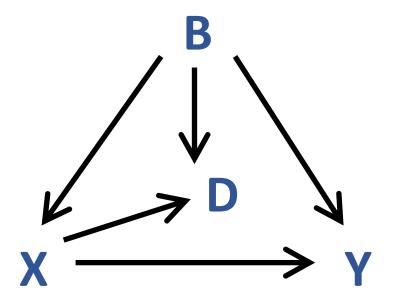


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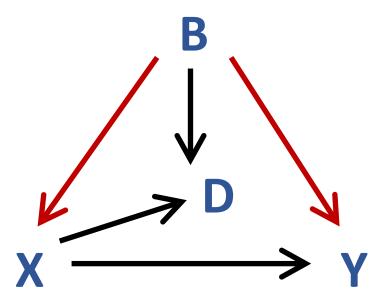


Backdoor path  $X \leftarrow Z \rightarrow B \rightarrow D \rightarrow E \rightarrow Y$  is <u>already blocked</u> by the collider B. If we did adjust for B, we could "re-close" the path by conditioning on Z and/or D. There is more than 1 way to de-confound the X to Y relationship!

### Game 3:



#### Game 3:



There is a backdoor path from  $X \leftarrow B \rightarrow Y$ . Need to adjust for confounder B.

# Simpson's Paradox (1951):

- Same (fictional) data
- 2 stories
- 2 different conclusions

Story 1: "The Bad / Bad / Good Drug"

	Control Group (no drug)		Treatment Group (took drug)		
	Heart Attack	No HA	Heart Attack	No HA	
Female	1	19	3	37	60
Male	12	28	8	12	60
Total	13	47	11	49	

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5% (1/20) women in **control** group had heart attack

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22% (13/60) controls had heart attack

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- → Drug is bad for women
- → Drug is bad for men
- → Drug is good for people

We know it is impossible for a "Bad/Bad/Good drug" to exist!
So what's going on here?

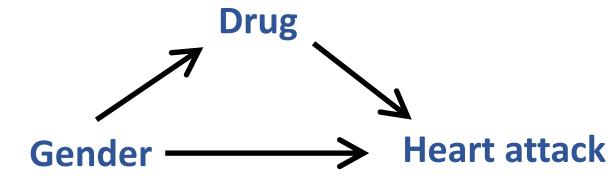
"In vain will you seek guidance from [the data]. To answer the question, we must look beyond the data to the data generating process."

#### **Data generating process**

- Gender is associated with Heart attack (men at greater risk).
   Gender → Heart Attack

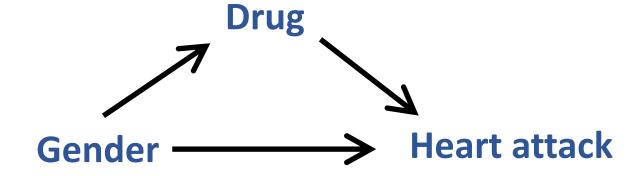
#### **Data generating process**

- Gender is associated with Heart attack (men at greater risk).
   Gender → Heart Attack
- Gender is associated with Drug (women had preference for taking Drug).
   Gender → Drug



#### **Data generating process**

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Gender is a **confounder** of Drug and Heart attack, so **use gender-adjusted estimates** of Drug's effect on Heart Attack and **conclude drug is bad**.

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#### To get average Drug Effect adjusting for Gender (a confounder):

Take simple average (because sample is split 50% men and 50% women),

**Pr(Heart Attack | Drug) = 
$$(7.5\% + 40\%)/2 = 23.75\%$$**

Similarly, Pr(Heart Attack | No Drug)

Therefore, drug is Bad! No more paradox.

Story 2: "The Bad / Bad / Good Drug"

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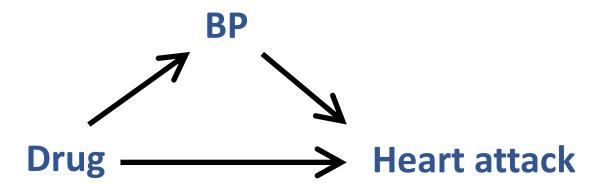
- Blood Pressure → Heart Attack
- Drug  $\rightarrow$  BP
- Drug → Attack

#### Data generating process (beyond the data)

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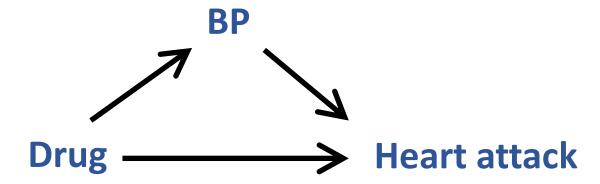
• Drug  $\rightarrow$  BP

Drug → Attack



#### Data generating process (beyond the data)

- Blood Pressure → Heart Attack
- Drug  $\rightarrow$  BP
- Drug → Attack



BP is a **mediator** of Drug and Heart attack, so to obtain an unbiased estimate of Drug's effect on Heart Attack **we should not adjust for BP**.

Conditioning on BP would disable one of the causal paths (maybe the main one) by which the drug works.

Story 2: "The Bad / Bad / Good Drug"

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#### We should not adjust for Blood Pressure, so we use the unadjusted estimates:

22 % (13/60) controls had heart attack 18 % (11/60) treatment group had heart attack

→ Drug is good for people

# Same data 2 stories 2 different conclusions.

Q: So do we aggregate data or partition data?

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A: It depends on the process that generated the data.

If Pr(Y|X) > Pr(Y), then X causes Y.

If Pr(Y|X) > Pr(Y), then X causes Y. NOT NECESSARILY!

If Pr(Y|X) > Pr(Y), then X causes Y. NOT NECESSARILY!

If we see X, the probability of Y increases. This could be due to:

i. Y causes X

$$Y \longrightarrow X$$

ii. Some other variable Z is the cause of both X and Y

$$x \xrightarrow{Z} y$$

$$X \longrightarrow Y$$

Adjust for as many variables as possible. It can't hurt. Throw everything in the model!

Adjust for as many variables as possible. It can't hurt. Throw everything in the model! WAIT!

Adjust for as many variables as possible. It can't hurt. Throw everything in the model! WAIT!

You can control for too much. Sometimes you end up controlling away the effect you're trying to measure by conditioning on a mediator, or you induce bias by conditioning on a common effect (aka collider).

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Inaccurate / insufficient definitions of confounders.

- 1. A confounder is any variable that is correlated with both X and Y.

  NO! Z could be a mediator  $X \rightarrow Z \rightarrow Y$
- 2. If you suspect a confounder Z, try adjusting for it and not adjusting for it. If there is a difference in the effect of X on Y, then Z is a confounder and you should use the adjusted value.

Inaccurate / insufficient definitions of confounders.

1. A confounder is any variable that is correlated with both X and Y.

NO! Z could be a mediator  $X \rightarrow Z \rightarrow Y$ 

2. If you suspect a confounder Z, try adjusting for it and not adjusting for it. If there is a difference in the effect of X on Y, then Z is a confounder and you should use the adjusted value.

NO! Z could be a mediator or a collider.

#### To learn more:

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A Regression Framewo

TELLE

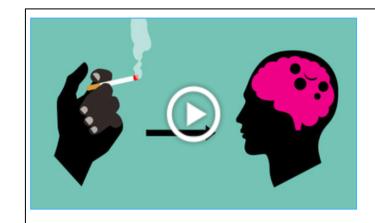




# A Regression Framework for Causal Mediation Analysis with Applications to Behavioral Science

Christina T. Saunders (D) and Jeffrey D. Blume

Department of Biostatistics, Vanderbilt University



# Causal Diagrams: Draw Your Assumptions Before Your Conclusions

Learn simple graphical rules that allow you to use intuitive pictures to improve study design and data analysis for causal inference.





